LEARNING MATERIAL

SEMESTER & BRANCH : 3rd SEMESTER CIVIL ENGINEERING

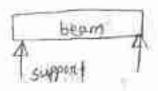
THEORY SUBJECT : STRUCTURAL MECHANIC (TH -1)

NAME OF THE FACULTY: ER. SUNIL KUMAR SAHU

12 Aug 2020 Reviews of basic concept shear force & bending moment of beam. * Beam :- It is a horizontal member which triansmits the lateral Louid. pours of [the * what is the obsective of beam ? The objective of beam is to transmit the lateral board to the beam and finally to the beam and finally to the use of beam.

The beam are used in framed structure. Bipe, water tank, cable, ruck, etc. * What is smuletune:- ! es a body 7 several element such as beams > which can sit up nesistance agrenest deformat by the applycation of external force . * on these of prom :-O simple supported beam

10 Gootileven beam ___ X0 x a weighting 1 beam @ Fined. beam @ Contineous Learn simple supported beam: - A beam supported on resting freely on support is known as simple supported beam.



6) Confilerer beams A beam whose one and is fixed and other and is fixe is known as confilerer beam.



(3) over-hanging beauting of end position of the beam known as over hanging boom-

contilevent beam

@ fixed beam: - The beam whose both ends are fixed is known as freed

beam diss could be built in beam

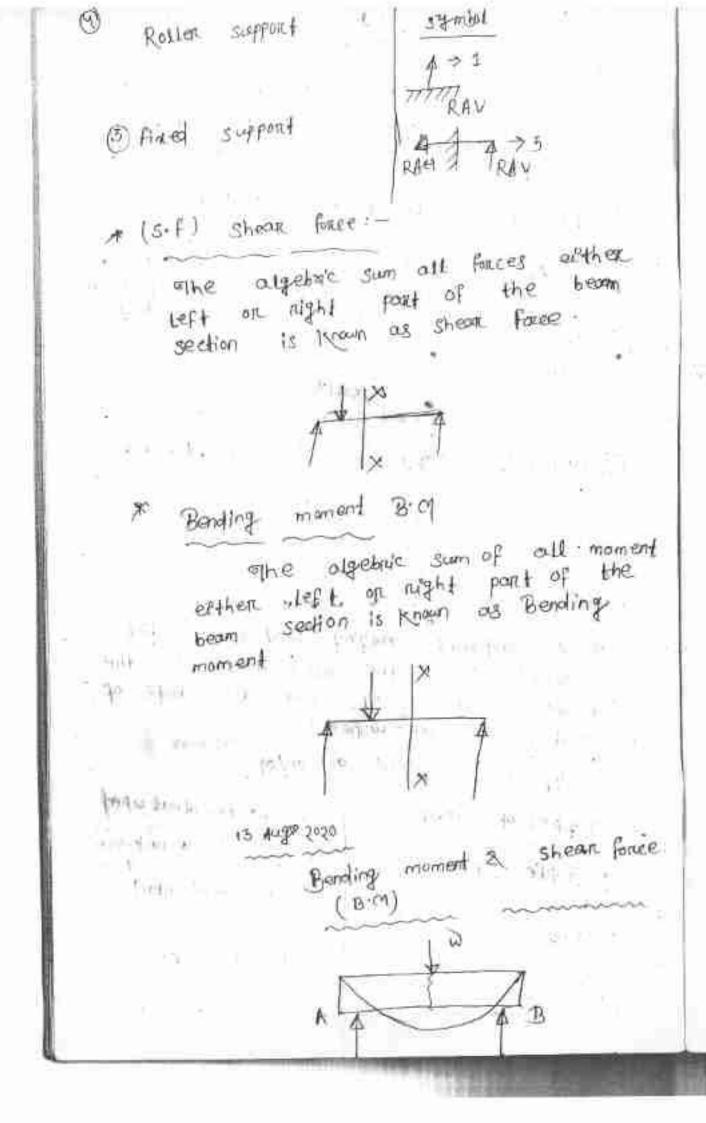
on and beam.

Continious beam :- It the beam haveing more than beam support is known as continious

states of road

@ point 1000 @ uniformly distributed wad

(3) uniformly variging bod (u.v.l) 1 Point bad :othe look which arts at a point is known as point load. 7 othe unit of point Bev or kov (+) @ uniformly distributed load (u.d.l.) 4 As conformity distributed is one which spead over the entitle length of beam In such way the mate of localing is uniform . (TSalm 3 uniformly vocaging used (aid!) (atter) > A uniformity varying boad is one which spead over the entire length of the beautin such wary that the nate of Leading is non-uniform. > It is expressed as or/or Reserton aleas uped TYPES OF SUPPORTS + 4 +1 No of unknown ? Each us simple support (PAH HOBIZONEN) o hinge support > 4 > RAV (voti en) >a



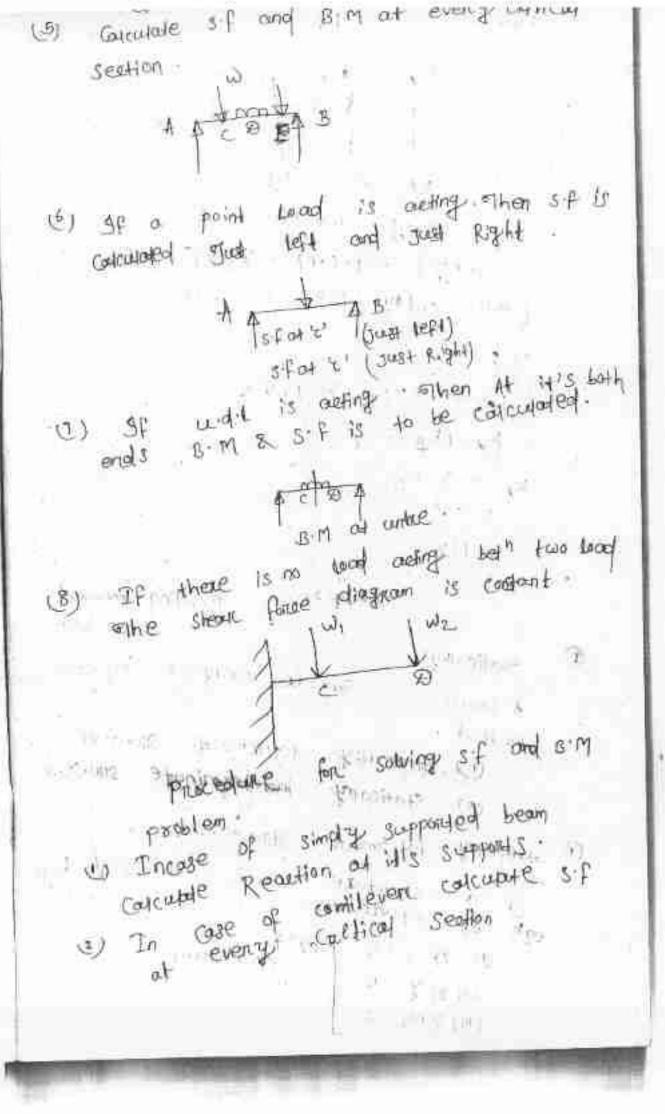
spef" of shear force > The algebraic sum all facess either Left of night part of the beam section. A X section is known as section sign convention of 3.1 sign convention of 2.01 sanging Hogging m = F x L distance | [N - m]

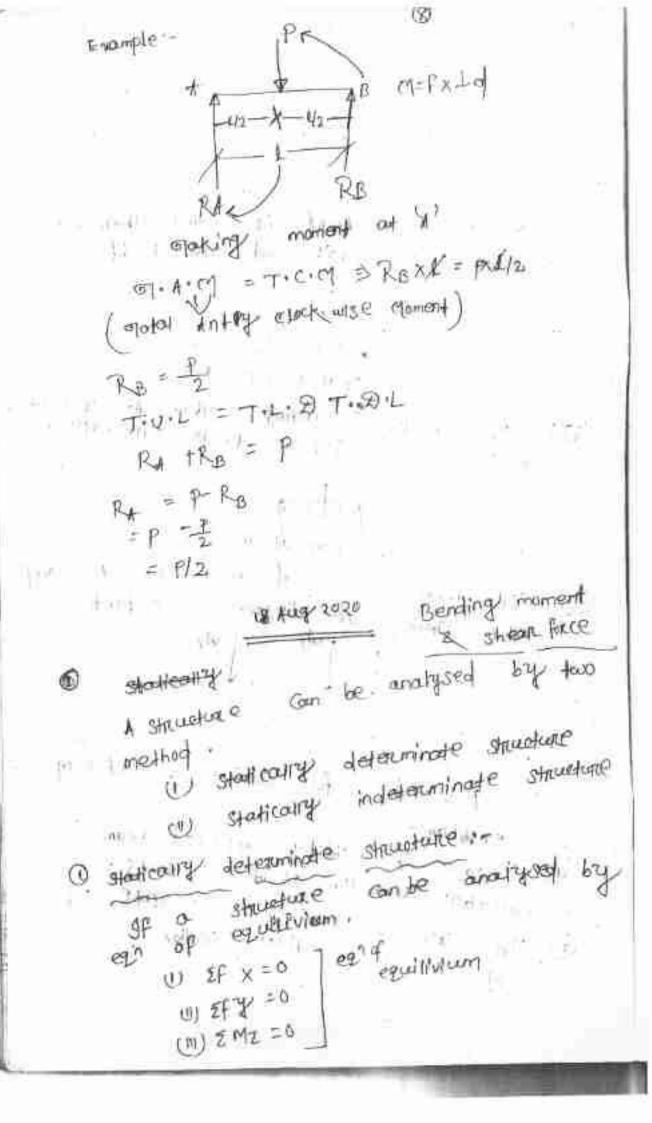
M = F x D distance | [N - m]

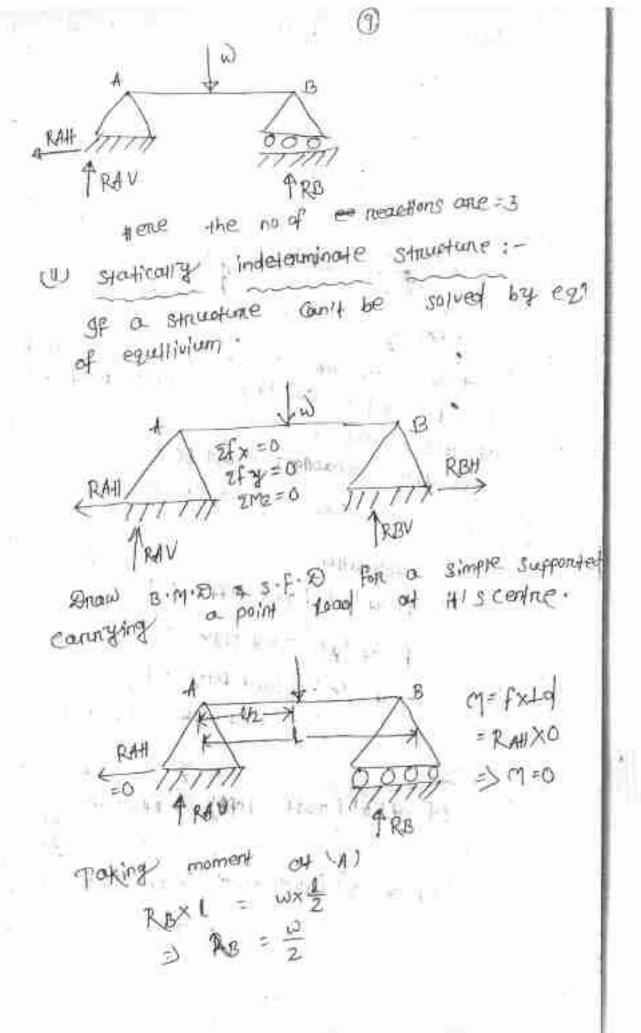
M = F x O = O

6 Shear Fine diagnam: - (S.F.E) . one which shows the variation of s-f along length of the beam. Bending moment diagram (B. M.E)

Bending moment allows norm is one which shows the rength of the beam . I'mp points to be Remembersed while drowing the BMB & S.F. B (1) The Length of the bending mamont diagnam 8 5.f.8) must be equal to ② othe shear fince diagnoun is alrawn below the booked beam diagnoun & below the shear below the shear force diagram. (3) In simply supported bean sihe bending moment at its ends is zeno. Si Não 8=0 1 In confidence beam, the bending moment at it's free and is zero B M at 8 =0







(10) Total upward Load = Total downward load RAV + RE = W DRAV = W- 2 -= w RMI=0 10 Let us consider a beam AB whose Length is it and countying a point Load (w) so the meaning will be RAU = 2 , R8 = 2 S.F calculation:-S.F at (A? (Just Left) = 0 s.f out (4) (Just Right) = 12 plat it st at ce! (just left) = + 1/2 (Sust night) - RAV-W sif of (s) (sust left) = RAV - W · 프 - 교 sif at (3 (3 with Right) = RANTRB-W - 光十些中一的

. 0

Berding moment Calculution. Bending moment 4 = 0 " " = +RAV XL/2 :+(芝) (B·M) = +4 B-11)

(Modimum)

Bendling of $B^{j} = RAVXL - \omega \times \frac{1}{2}$ $= \frac{\omega}{2} \times L - \frac{\omega L}{2}$ B FAM(+t) HERE THE SA (s.f.2) (--) (B.M.D) Maximum Bim occurred where the shear fince (m.weng) 15 Zexo)

I simply supported beam countying uniformity distributed load throughbut the length of the beam we

O= RAIR L ARB . WILL TOKING moment of 4)

J. 4. 4 = J. c. 4

> RBXE = DXXX

> Ro = t = 1

We know that there is no load auting in nonzontal direction so RAH. = 0, we have to calculate RAV =

T. u.L = T. D.L

= Rot RAV = WL

 $\Rightarrow RAV = \omega L - \frac{\omega l}{2} = \frac{\omega l}{2}$

Sif Calculations -

3. f A + A (Gust 1971) = 0 .

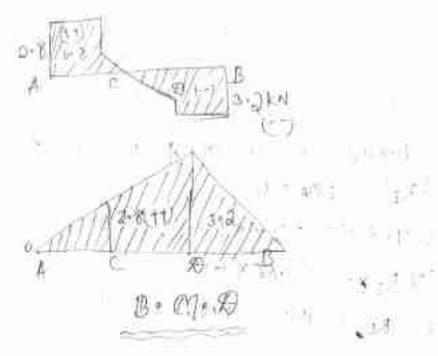
S. FAT (A) (Just right) = + wl

s.f At 81 = 1 - 1 = 0

s.f at 13 (just left) = - wil

Sf. a4(B) (JR) - wy - wy - w1 = 0

```
3.f calculation :-
       s.f at (1) (3.1) =0.
    st at 11 (J.K) = +2.8 KM.
        s.f at 'E' (J.L) = + 2.8km.
         3. fod te' (J.R) = +2.8 KN-8
                        = 0.8 KN .
         3.f of 201 (J.4) = +2.8-2 = 0.8 km
          sifor 8 (J.N) = +2.8-2-4
= -3.2KN
 =+2.8 -2-4 =-3.2KM
         s.f of 'B) (J.R) = (+2.8 + 3.2) - (2+4)
                     = 6-6=0
       B. M at 4' = 0
      B. Mat 'c' = 1 (2.8 x1) = 2.8 kn-m
      B-M at 21 =+ (2.8×1.5) -(2×0.5)
      13. M of (B) = (28 x 2.5) - (4x1+2x1.5)
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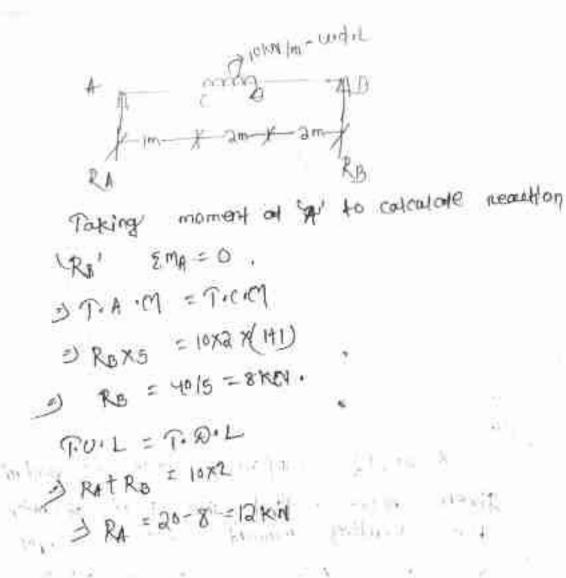


10/16

simply supported beam is loaded given below. Find the point of which bending moment will be maxim also proces B.M.D & s.f.D ano bom . the

11/4 10

Prub-2 Straw shear force and bending moment lagger for the beam indicating the value of marking bending mamment. The leaded diagram of the beaming given her ray a Rightige from peron ,



Calculation of 39:-

(y) s.f. on (x) (Just Lept) = 0

(y) s.f. on (x) (Just Right) = +12 KM

(y) s.f. on (x) = +12 KM - (10 Kg)

(y) s.f. on (x) = +12 KM - (10 Kg)

(v) s.f. on (x) = +12 KM - (10 Kg)

(v) s.f. on (x) = +12 - (10 X 2)

(v) s.f. on (x) (Just Lept) = +12 - (10 X 2)

(v) s.f. on (x) (Just Lept) = +12 - (10 X 2)

Bending moment
$$(200)$$

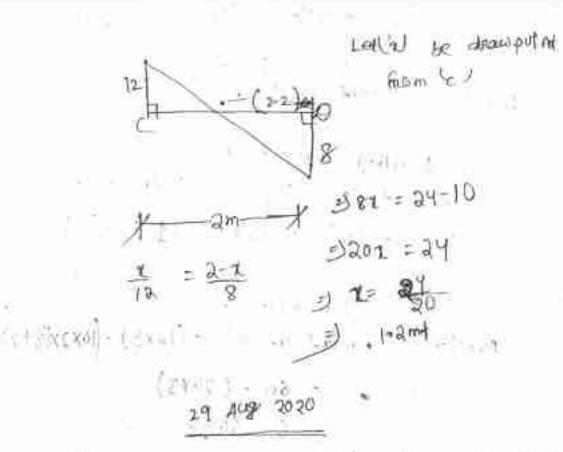
Bending moment (200)

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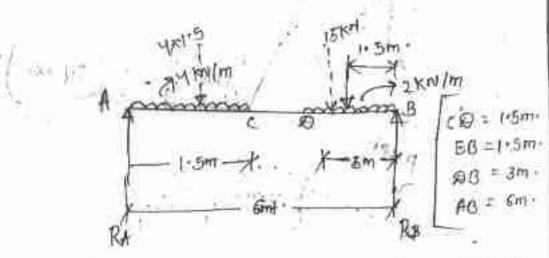
Tepa?



A simply supported beam AB = 6 ml
Long is bearled as shown in the
Long is bearled the s.f. B and 18.14.D

Righte Constant the s.f. B and 18.14.D

For the bear ALSO final the position
and volume of maximum B.M.



3+0P-1 Taking moment at A, 5 MA=0

Total anticlokuise moment

Total = T.C.M (G-4.5=1.5m.)

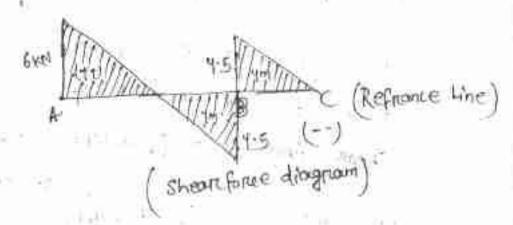
```
> RBX6 = 4x 1.5 x 
                                                                                                                                                                         ( 1.5+ 1.5 t1.5)
                                => RB = 54 = 9 KN
                           Step-2 Total upword wad = total Downward
                                        TIUL = T.D.L
                                    => RA+RB = 4x115} 5TRX3
                                RA = 17 - RB
                              =17-9 = 8kN

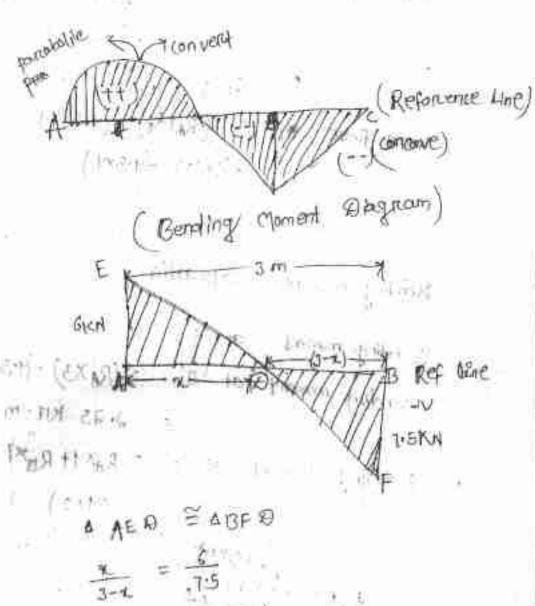
= 17-9 = 8kN
                      step-3. Shear force s.f calculation
( Just Left) = 0
                                                SIF OF A) (Just Right) = +8 km
 S. F by . c' = 8 - (4x1.5)
                                                 = 8-6
= 2 km
                                             Shear force of E' (Just Leps) = 8 - (4×1.5)
                                                                                                                                                                                  -(2x1x5)
                                         s.f of CE! (Just Right) = 8 - (4x1.5)-(2x16)
                                                                                                                                                               = -5KN
                                          3.5 of B' (J.H) = 8 - (4x1.5) - (2X3)
                                                                                                                                                                                                      - 5KM
                                                                                                                                                               - - JKN
```

```
S.F at 43 (J.R) = (8+9) - (4×1.5) - (2×3)-5
             MAKALM
         RA = 8KM
          Bending moment calculation
         B.W 64/47 =0
          B'M at c' = RA X 15 - (4x 1.5x 1.5)
                      = (8 x1.5) - (4x1.5x0.75)
        13. May 401 = (8×3) - (1×1.5×(1.5+ 1.5)
                 = 10.5 KN = m
Bending moment of E
```

7th Sep 2020 and period Munday as shown in the figure draw sig & B.M. diagram of the traded beam. Aind the point of controfference and A francour of francour. -3m- + m-x point of contrafference the point of which the bending (to to -ve) and changes it sign (to to -ve) and vice - version # frammer Jangermaner RA = 5M RB = 12KM To And RB erjaking moment at A = Em =0 RB X3 = 4.5X 4X (1/2) ≥ Ro = 36 = 12 KM To Find RA T:U.L = T.D.L # RA TRO = 4.5x4 Pu = 18-12 = GKN

```
Shear force Calculation:
 shear funce at (A) (Just Left) = 0
 Shear forme of (1) (Just Right) = 16 km
  Shear force of B' (Just Left) = +6KM-(4.5X3)
                        = -7.5KN
 shoon force of 8 (Just Right) = (RytRs)
                - (4.5×3)
             = 6+12 - (4.5 /3) : = 4 5 KN
Shear force at ("RATRE) - (4.5X4)
         =(6+12) -(4.5x4)
 -mark 1 -0 -1
 Bending moment Calculation.
Bending moment of 4) = 0
  Bending moment of B' = (RAX3) - 4.5x3 X1.5)
                     = - 2.25 KM - m
   Bending moment of c' = RAXY+ Rux1 - (4:5
      ( Loaded Diagram)
```





$$x = \frac{18}{13.5} = 1.33$$

$$E B \cdot M_{X} = 0$$

$$E RA \times y = 4.5 \times y \times \frac{y}{2} = 0$$

$$6 \times y = 4.5 \times \frac{y^{2}}{2}$$

$$6 \times y = \frac{12}{4.5} = 2.66$$

$$4.5 \times y = \frac{12}{4.5} = 2.66$$

$$2 \times y = \frac{12}{4.5} = 2.66$$

$$2 \times y = \frac{12}{4.5} = 2.66$$

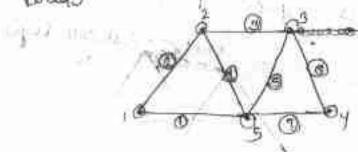
$$3 \times y = \frac{12}{4.5} = 2.66$$

Trusses

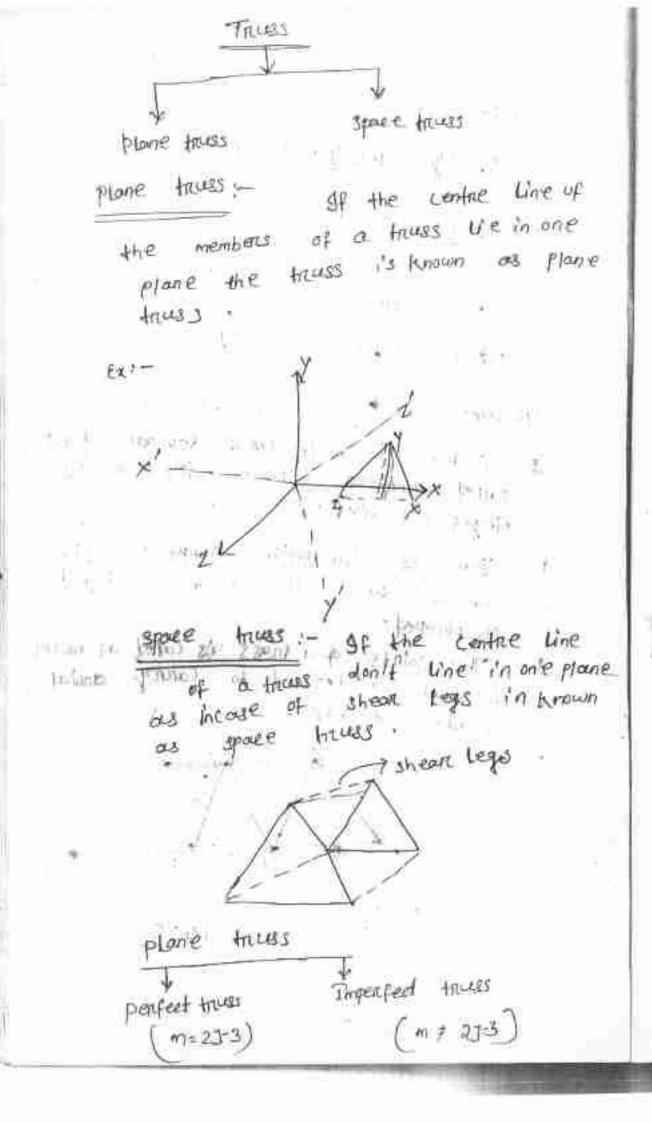
A threas 1/13 made up of several balls
control members while he together by kinges or and.

But for concurrentian purposes. The Juineds are supposed to be highed x out bluebid.

more othe joints of a truss is could as modes A truess is designed to contry anday Loads of ends



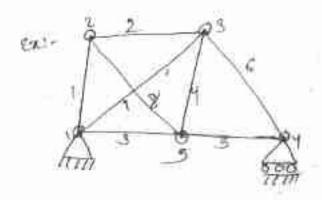
MO OF member = 7 " gotata (mades = 5



(i) Penfect thouss :- A thouse is sould to be imperifert it don't sodisfy the eq m & 23-3 81' m=23=3 NO of member (m) = 5 U Joins DJ & 4 Employetta 12" Antari https://www. 1.4.9 (m) = 5 R. H'S 23-3 = 2x4-3 = 8-3=5 L.H.S .. = R.H.S So H is perfect trues . 11/11/1981 (ii) Imperifert truss :- A truss is said to be impensed if ident, satisfy the 2 × () 10 () e27 Trackings m + 25-3 1 a 1 o

m= 2]-3 L. H'S = 2J-3 = 2×4-3 =8-3 =5 L. H. S LR. H. S / L. H. S + R. H. S so it is imperpent thous Impenfect Hauss Redundant Deficient trus thus m72J-3 m < 71-3 _ 1611-51 Internally Engenrally 2111 11 his 18 + Redundant Redundant trugg dicers of the second in the second of I Deficient thousing of the number of members is less than the negul--ned that mx 21-3 that type of thouss is called as Deficient thouss. Ex. !-

no of member = 4 11 30/ml = 4 L. H'S m = 4 .K. H. S = 2J-3 .. = 2x 4-3 =8-3 - 5 (ii) Redundant trues :- If the number of member is more than the neguined 1.e m> 21-3 No of , M = 8 NO # J = 4 1 1870 95 LIH'S = 6 The Roll Sun 5 23-3 = 2x4 -3 Internally Redundant truss - of the number of members is mone than the nequired , i.e mz 23-3 ghis type of thuss is known as internoung Redundant truss.

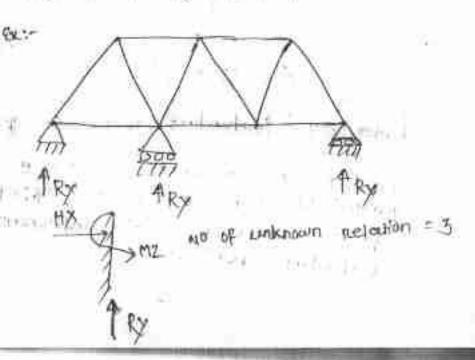


No of member (m) = 8No of Joint (J) = 5 $m \neq 2J-3$ L.H.S m = 8 R.H.3 = 2J-3 = 2x5-3 = 7

30 14 is intermally redundant thouse

Enternally Redundant titless :-

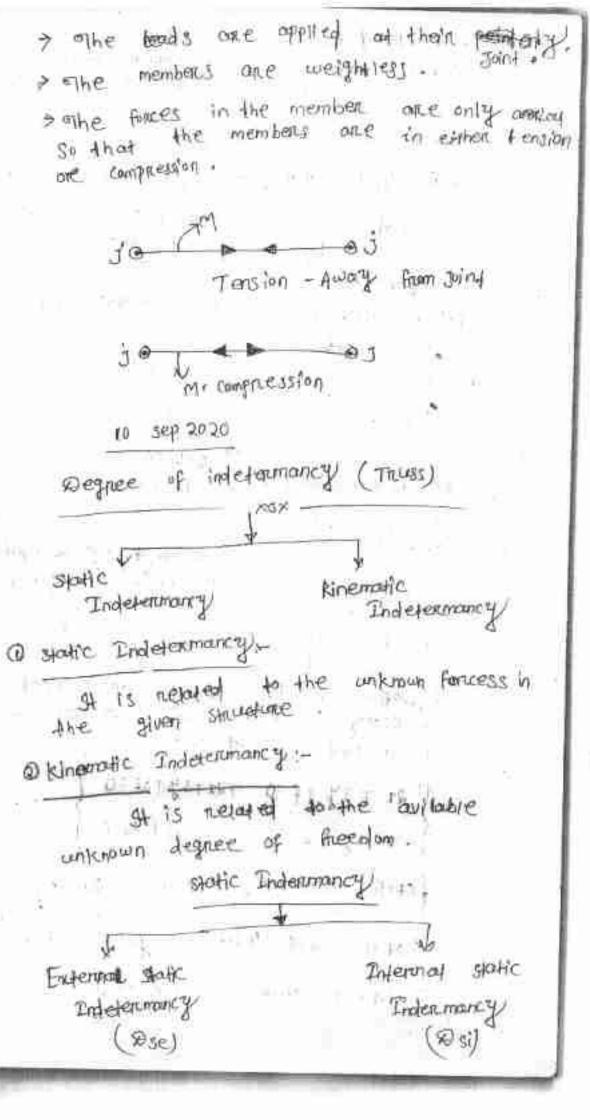
than 31, Then The bruss to could as entermally Redundant truss.



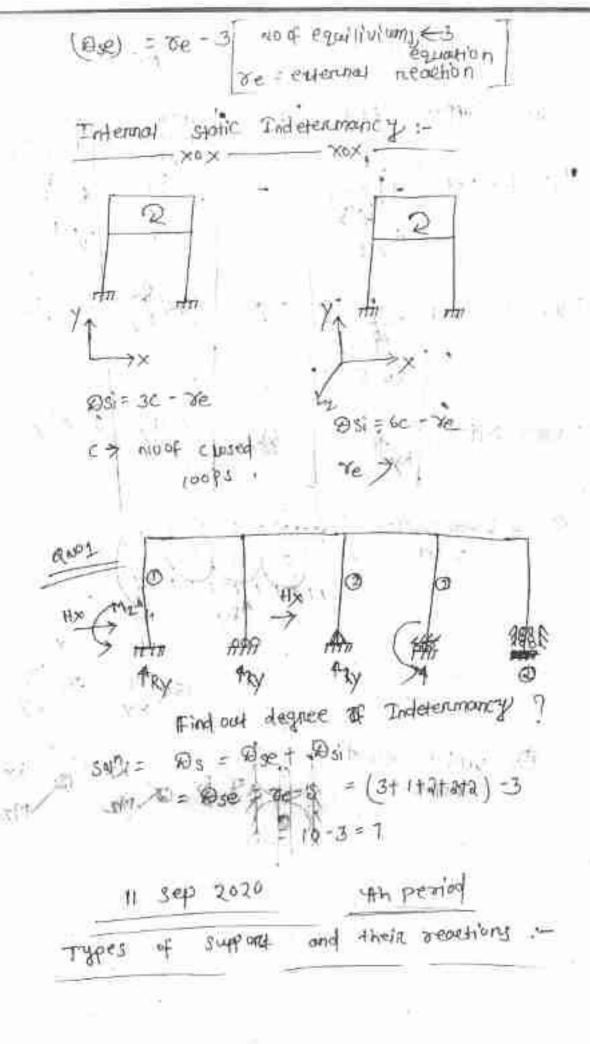
d 765 30 50 = /: Here the of meachions = at It = 4 nos. 4 > 3 soit is an Externally nedun -down + times. Billion Plane fruss WI ARREST Englis Tinci Impensed thruss plenfell houses (m + 23 3) (m = 2J-3) Deficient Redundant towers muss (m >23 3) m 123-3 TOTAL PERSON THE PARTY OF THE P Endermonly Intermoury) Redundant Redundant truss muss (m= Reaction >3) (2.15) Bullet.

we know that Intake of 30 In case of 12 na of equilibrium eq no of equilibrium eqn = 6 ST NUMBER OF 8 = R-6 -1057.8 R = no of Reactions 8 : degree of determoncy

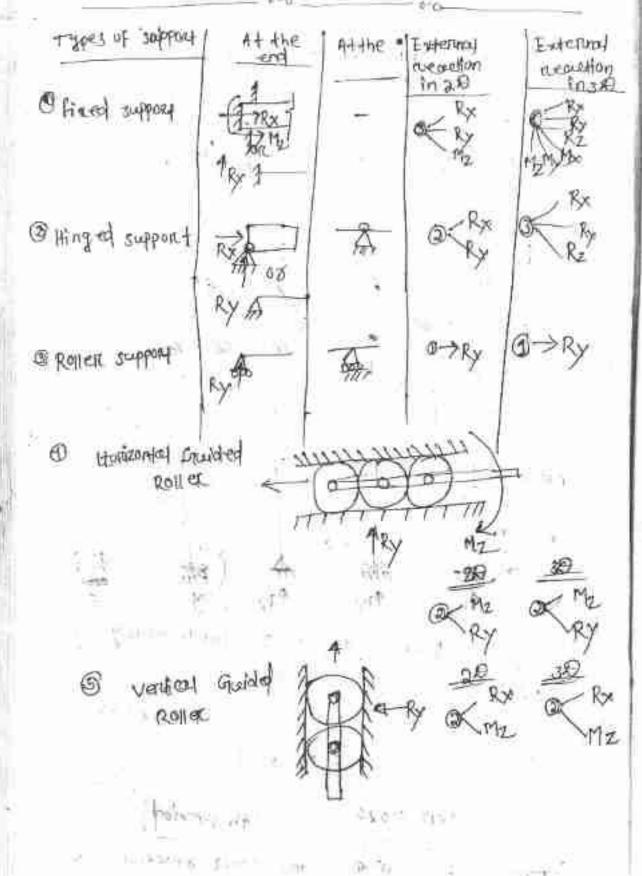
\$ F @ = 0 , \ \D = R-5 i.e woof available ext = no of weknown negetions . The structure win be stable and determind @ >0 : [other structure will be stable and indetermined] (3) If DCO, [The structure win be unstold and deferenting ti Supports (timed supposeds WO of continound Reaction Roller (b) 82 F 32 e) Hingel supposed tooks Assumptions = plane thuss:to solve are in one plane the members connected of then members ave ends by smooth hinges



7 St is metated to unknown > St is neloted to external support reaction, unknown Tricken) nearting of member forces - motor state indeterminely (2) = 200 + 25; end static Independency - The structure is could staticolly descriptione it can be analised by willing equation of equiliviam. Equi of equilivium in Equi of equilivium in 38 28 @ ZF 1 = 0 , @ ZF 2 = 0 @ 7Fy=0 @ Efy =0 @ ZF2=0 @ zmz=0 @ 2MH =0 The no of Equation of @ EMy =0 equitivium istath @ 2 m2=0 cose of 38 othe no of each of equilibria -m is lat in loge of 310 O If the given structures members cannit be analised by using equilivium equations . Then they are conted as statically Indeferminate structure of Redundant structure. tropp His 32+47 +8=0 4x+6/+82=0 static indemonity = unknown - known Plotal static Indetermancy (Ds) = Oset Dsi "HOLE IN SIGHT Enternal static Independently 1-



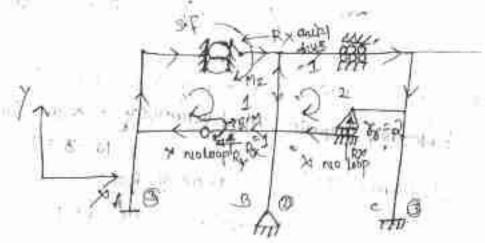
on



92 Find the degree of static indomnancy of given frame as shown in the figure below. TITE 韧 Total skutte Indefinency Ds = Dset Ds; Endenthal static Independency - Dise = 7e-3 Interval static Independent - Doi = 30-88 c > No of closed 100 ps € 7 Rejeaseel Reaction Psi = 30 -88 (C=0, 88=0) -3x0-0 +0 Total static Indetermancy Ds = Det Dsi = 110 = 7 Degree of static indepartments 4, 1, find the degree of static indexmency of Short State Weller Qs = QsetPsi le Cristi 8e-61 10 011-@si = 6c - 88

DSI = 3x1 =3 D3=5+3=8 Digree of indeference = "11"

Find the degree of state indeterm--ancy as shown in the figure betow .



12 SQ 20 111

State And Acts

Did = Demograph store Tryon

· 65

ive of closed larges redesed ne and pr

total state indetermancy

 $\mathcal{D}_{3} = \mathcal{D}_{5}e + \mathcal{D}_{5}$

Ase = Enternal static indetermance Osi = internal static indutermenty Dise = re - NO of equilibrium equation

= Te-3 ['se -enterinal medefion

1.1

Static & Indemoncy in pin sinted structure
Degree of

By P_{S} P_{S} P

J7 NO of Joints

sin - Ds = Dset Dsi

Ose = re-3

re = 211=3

Die = 3-3=0 The housis extendity

Asi = m - 2J+3 m=7 J+5

m-

tun

```
Just = 7-(2×5)13
      = 7-10 13
      =313=6 ( Thethuss is internally determinate)
    Total static Indetermancy
             z Dset Dsi
             That, means . The thruss is stationly
                2Fn=0 17
    determinate.
                Tfy =0
                 EMz=0
   of the given truss as shown in the
the red
    figure below.
          20
      Total static indetectioncy
        Die = Ve 3
            = (3-3)=0
         The toward is Endermoney determinate
              m+-an
```

 $Ds1 = \frac{m+3}{m-2j+3}$ $m = 10 \qquad j = 6$ $= \frac{10}{(-2)+3} \quad 10 - (2 \times 6) + 3$

= 0 +1

```
The truss is internally indeterminate -
        Ds = Dse+Dsi
 - ot1
   The truss is dequee of indetermoney of '1' -
   Analysis truss: - The analysis of truss is
      don by the following methods
(3) Promotion Method Treeling of Joins
       1 Grouphical Method Ly method of seedle
    Charles Date of
 1 Method of Joints :
   procedure determine the support reactions
         in case of simple supported thuss.
     > consider any joint with minimum unknown
     members meeting at that soln is not
      greater than 2
  > assume on the forces in the members
     one tinsile in notane - But if after
 colculation the value of member forces.
     concest - versive it is compressive in
put the next calculation of member
  forcess.
   > use equilivium equations or corditions/
     to get the unknown member forces.
                    Efy=0
```

Repett fint other joints . all find the forces in the members (Ac' 'AD' BE and 'BC' by wing method of joints of the given truss as shown in figure . LOKN we know that 41 inclined lonce has tono combonents . . . @ HorrizonHal Component 1 ventical component A.Fsino 7 7739 veretical. componed A Gland (6) makes with horst zontal :- Harrizontal Y component \$5,500 AF1 (1,1) 4F2050 42 Sales Service 91 F40004 F4090, 0 Maria Maria F100.501 TI COSE 75.3 10.11 rayshoy X Fy IF SSIFE 3

-

Find out the member forcess given thouss -

method of

5017 :-

statically indeterminate 95 = Psi + Pse

0 se = 6e-3

851 = M- 27 t3

Dse = re-3 Termonia notes

Ose = 184-3 = 3-3 =0

other means the hoss is externally

aleteraminate.

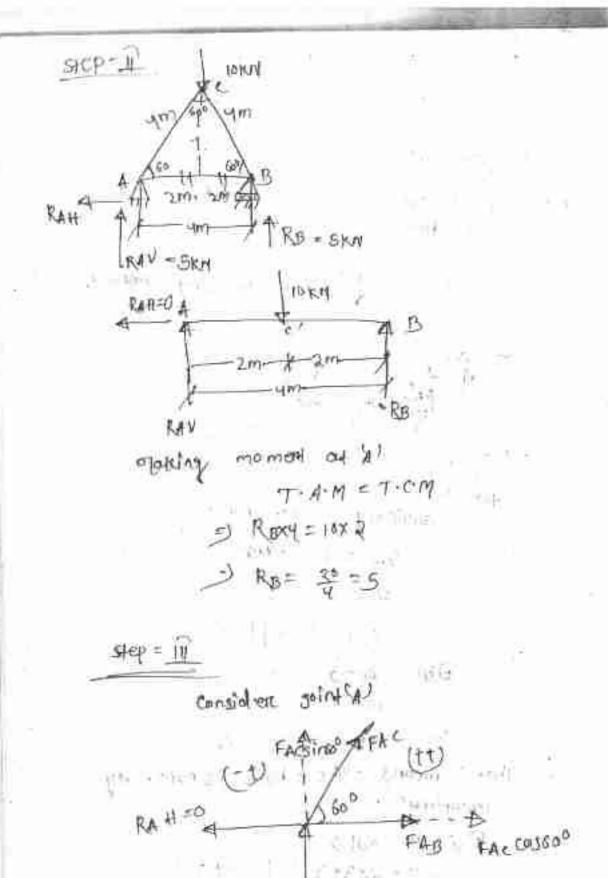
Psi = m- 73+3

-3-2×3+3 = 3-6+3=0

The truss internally determinate.

Ds = Dset Ds1 = 01,0

so the truss is statically determinate.



Manager Street

```
21-4 =0
   FAC singo tRAVED
  => FAC = -5/singo* =-1.776 KCI.
    = FAC = - 1-667KN
            = 11667 KN ( compressive )
       put the value of fac in the ear of
       FAB + FAC 1 4560 =0
      =) FAB - 1.667 × 605600 =
          FAB =
   Consider Joins (BU:
                      A FBC Sin 600
                  600
2 fx=0 , zfy=0
 - FB C COSGOO - FAB =0
- (Fox (0360 +FAB) FO
  J FBC (0500 + FAB = 6
   J FBC = FAB
```

THE ATT SE

= 5N (compressive)

Force in members	mangitude	Nature
FA C FB C	3, 66N	Compressive Trensile

By Determine the fince in wall the membras of the given hous . TRAV lus 3 m Say You a = Bo 9 Jero =3) 0= 4m (3) > 0 = farr (1) = 450 that static indetermancy 0s = Oset Osy Exiternal static indetermancy Ose= re-3 we = No of unknown beautions Que = 3-3 = 01 So the trussis externally determany. Internally static indetermanty 2s1 = m-2Jt3 m> no of members ! philos foon <5. DSI = 7-2×5+3=0 so the triuss is internally determinate Ds = Dse + Qd = 010 =6 so the thouse can be solved by the conditions of equilibratium.

```
Taking moment of A 1 ZM4 = 0
          T. A. M = T- CM
       >> K6 X2 = TODOX3 + 3000XR
       ) Re=600 N(+)
    RetrAH = 0.
   RAH =- Re =- 6000N(+)
        . 6000N(4-)
     RAH = 6000 N (4-)
      RAV = 4000N(1)
 Step-111 consider the John
      ( t) FEA 4 (t)
     Re=6000N IF FED
ZH=0 , 2V=0 ZH=0
       RetFES=0
  50 0001 4 FED = 0
     DIFER T - 6004N
     > FEB = 600 on (Comp)
     2V=0
    FEA = 0
          zens/null fince member.
no semigraphic par
```

23 Sep 2020

method of section

procedure to solve a truss by method of section !-

step-1 Fine support neactions if neguin

Step-I Identify the members and high - Light it in FBO of tracess.

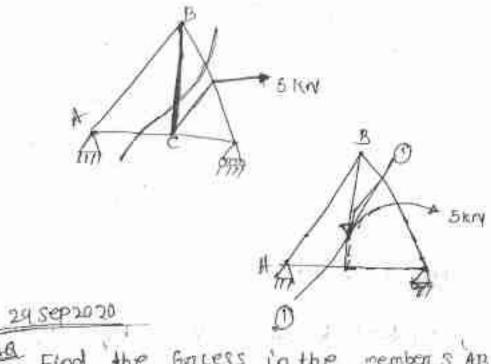
step-II Divide the entire truss into two parts but not cut mone than 3 members at a time.

Step-10 Mark the consider porchion with line and other point in dotted wine .

Assume all the forces one tensile nature.

step- vi Apply egn of static egullivi um EF# =0 5

ZF2 =0



18 Find the funcess in the members AB Be & ca of the focus in the figure

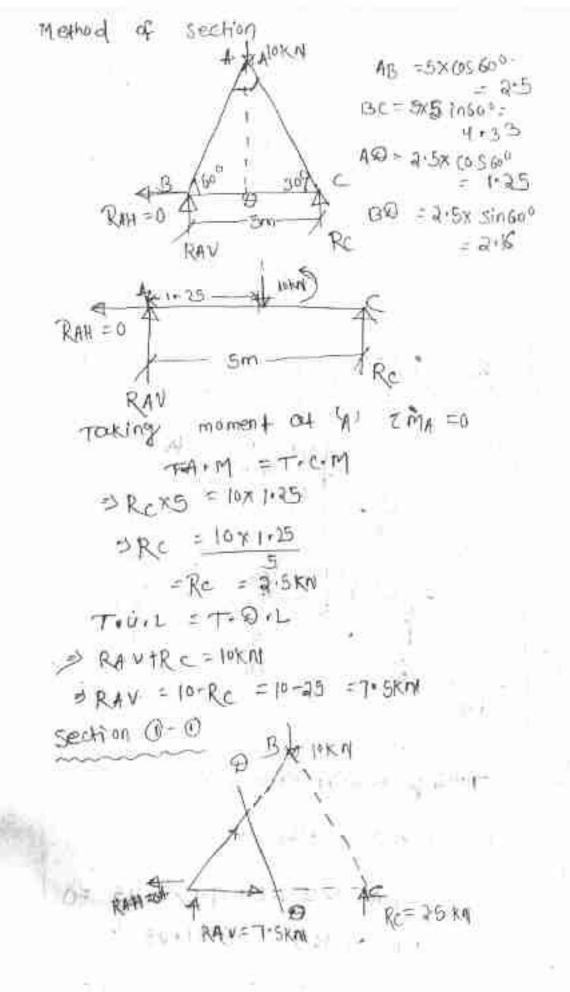
TENER The Literal · Pront Hord 9 - D

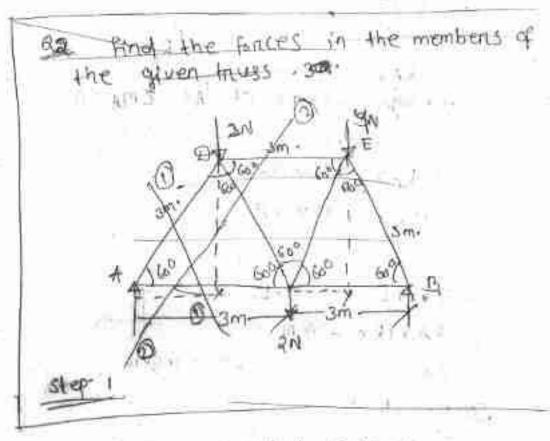
Total static indigen manicy Ds = Dre + Dsi

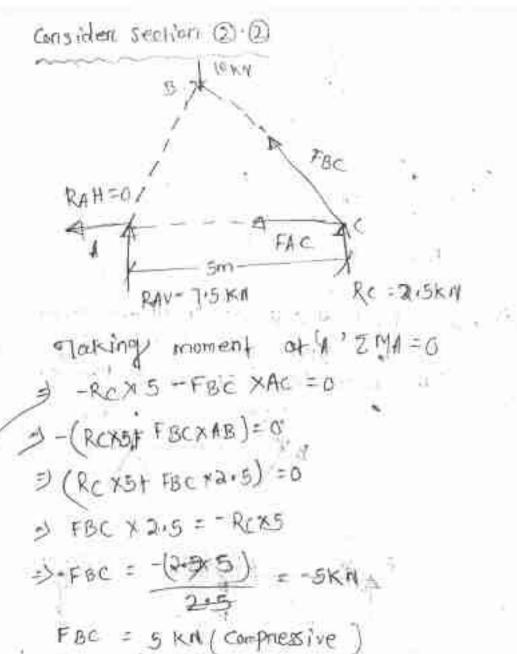
Englennal Static indetermony) Dse = Te 3 1 = 211-3

or Filting 5 The truss is intermally determinate 95 = 950 + 951 =010=0

so the trues is determinate.

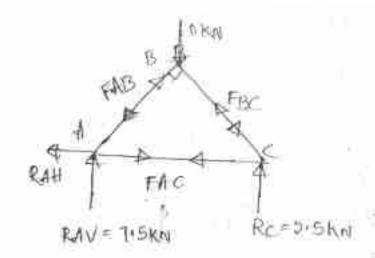




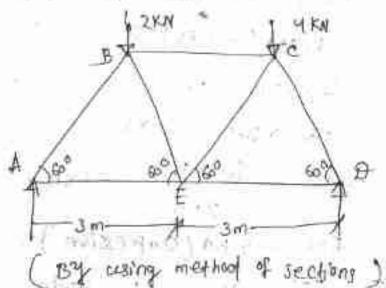


AB	8 - 66 1 <n< th=""><th>Compriessive</th></n<>	Compriessive
		21.06
AC .	4.33KN	Tensile.
3C	3 KN 1 17	Compriessive
	AC 3C	The lives I divers

K)



Find the forces in all the members of the ginden (beam) indicating whether the force is compressive on tensile.



m/1=900 -

Total state Indeter maning

1 x= 30560° =I+Sml BX=3010600 =2.5984

.. Ds = Dse tDsi = 3 05600

Enternal static indetermanty cy=35in600 Dse = re-3 =2,59971

Internal State Ditermanty, 9si = m- ajt3

= 782×5 t3

=7-10+3=0

Consider Section 0-0

TO Find FAB TME = 0

> RAX3 + FAB x 3 SINGO = O

2.5x3 / FAB > 2.598 = 0

1 FAB x 2 -598 = -2 -5x3

=) FAB = -(215X3) =-2.886 KN

FAB = 2.886 KN (Compressive)

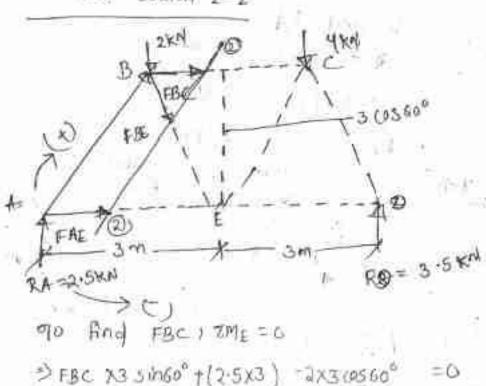
TO FIRST FAE , TMB = 0

R+ X 3CASGO - FAE X 3 SINEO° = 0

> FAE = 215 × 3 (45600) 3510600

> = 2.5 x 1.5 = 4.330 KN (9005178) 2.598

Constdet section 2-2



> FBC X3 sin60° + (2.5x3) - 2x3 (0560°

1) FBC = -1:732 KN

FBC = 1.732 KN (compressive)

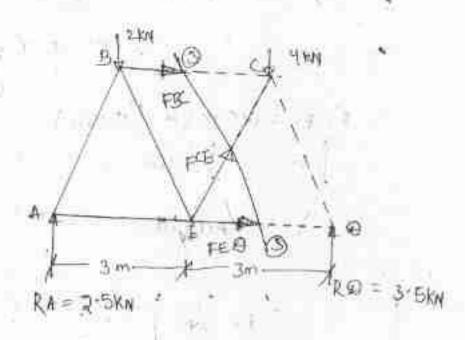
The find FBE 201c=0

FBE x 3 sin660 - (2x3) - FAE x 3 sin660 + 2 sx4.5

FBE =
$$\frac{-6}{2.598}$$
 = -2.300 KN

FBE = 2.300 KN (Tensile)

29 sep 2020

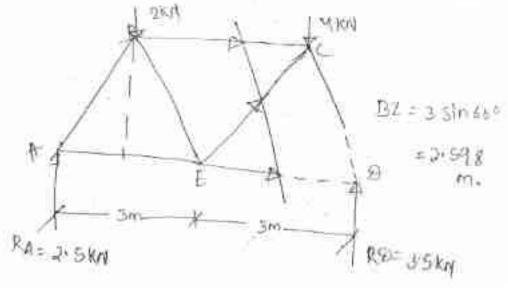


consider section &- 3

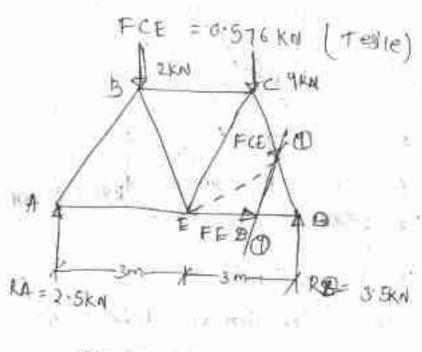
Let us consider the left postion of the thuss of the section @- @
To find FEQ; EMC=0

= (2x3) - (FED x2.998) + (2.5+4.5)=0

= FED = 2.020 (Tensile)



*Taking moment, of 48 / 2MB = 0 D-FED X2.598 TRAXI-5-FCE72.598



FCE > 13.09

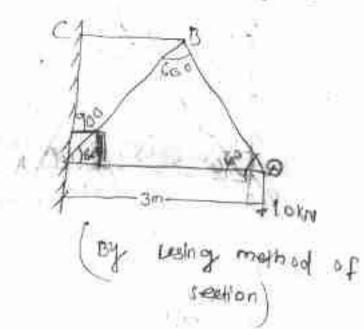
ST	forces in the	Magnificide	natune
9 9 9 9	FAB FAE FBE FBC FCE	2.886 KNI 4.830 KNI 2.300 KNI 1.732 KNI 2.020 KNI 0.576 KNI	Tensile Tensile Compressive Tensile Tensile

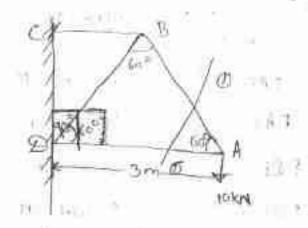
30 SYP 2020

6.83

598

Hven thus 13 shown in figure.



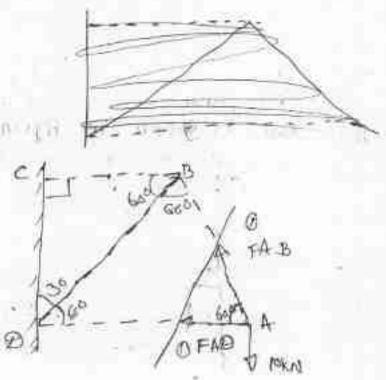


300

m/CDA = 900 - m LBDA = ADO-600 = 300

Consider section 0 -10

Let us consider the night part of the truss of the section 0 -0



AX = 3 (0 560 = 1.5m.)

BX = 3 4 n 6 0

= 2.599m.

= 10 find FAB EMB=6

> 10 Kn X 3 (0.5600 FAB X3 Singso = 0.

SLAM	forcesin-the member 9	Magnifude	mot une
0	FAB	11.54 KM	tersite
U	FAQ	575 KN	Compaessive
(m)	FBC	11-54 kg	tensele
(m)	F 80	11. 67 KM	compressive
97.7		30 kg	

1 110-2635 A linewas of that span and I say high subjected to the point could at B and 8 on Street in the Figure product the forces in all the members of the strand upon by method of smillions and method of justs and imposing both the method NXR Book bn 0 = 0.79 0 = tan-1(0-75)tans 153au static indictermancy (95) 6 040 = Dset Dsi 2000 = external static indetermounty = ve-3 Ke > Extensed nepethor Total external reaction = 2+1=3 Ose = 3-5=0. (So the truss is externally) Ds: = intermently static indetermancy Dsi = m-13 to m-+ no of members.

=6

W

ive

J-+ No of Joints.

25 = m-27+3

-5-2×4+3

-5-8+3=0

50 the thruss is intermining determinate

Ds = Dse + Dsi = 0+0 = 0

So The thruss is statically determinate

Structure.

Step-II SO HA = SKNI4 And Ve slaking + moment at 11) 1013 9. A.M = 11.C.M Vexy = 8x1.5 To find -VA "Total epwand load = golal down -- word todd minter into

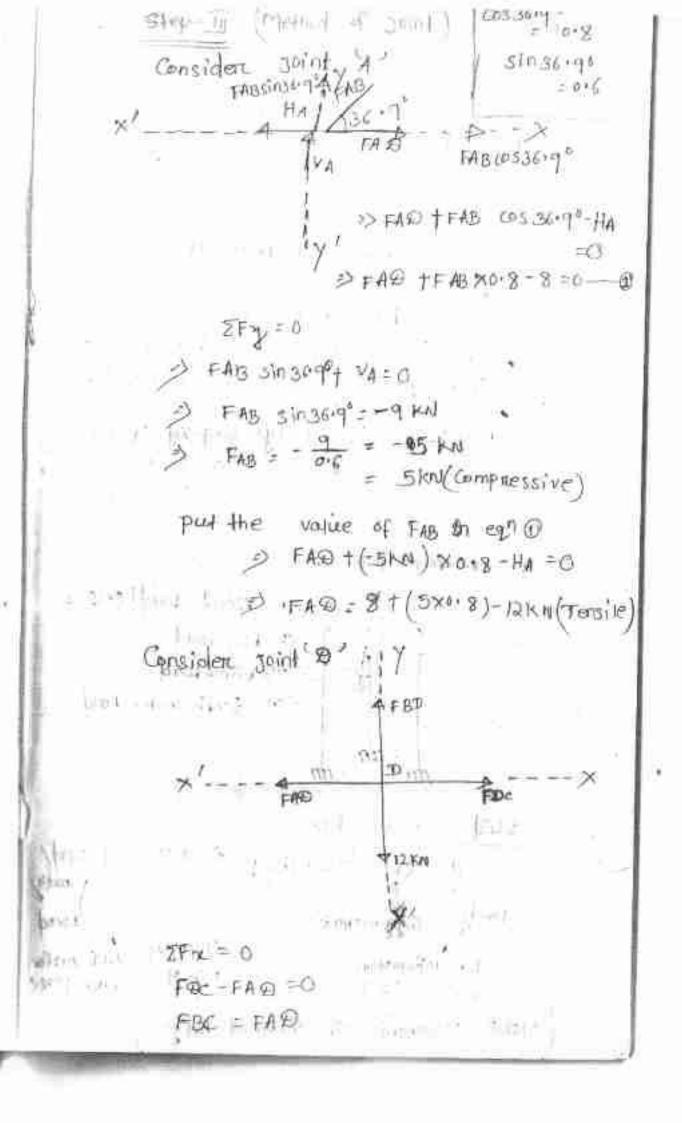
,

11.75

VA + Ve = 12KN

M. N. .

= 12 km = 3 km = 9 km (1)



FBC = 12 KN (Tenshir)

ZFY = 0

FBD-12 = 0

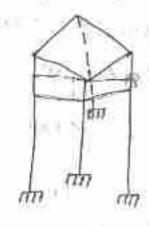
FBD = 12kn (Tenshir)

300t 2020

Strevetural electronics of solar

Mischanics - The study of forces, energies and their effects on various type of body is known as mechanics.

Structure: - It is a body composed of various structured elements such as beam - Collins, stab, footing etc. which can set up mesistance against deformation with the application of enternal fince.



(1) Dead Load (Serfwy)

(1) Wind Lead

(1) Earth welke Load

soled is two types

U) Rigid soled / body () Offormed solld/

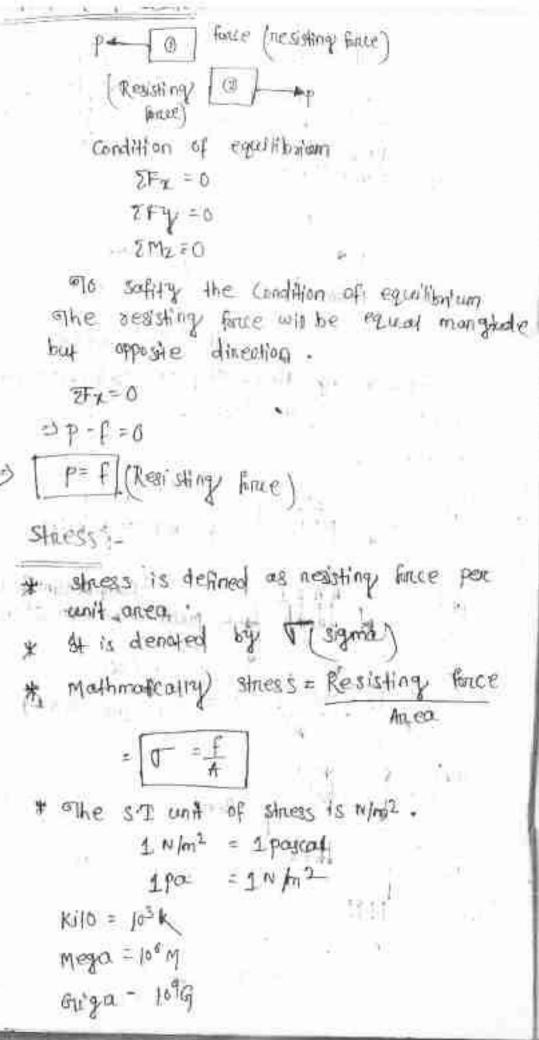
Lood Engly mestantes

no deformation

SM/M.OM MORM Deformation takes place

MOBB -> Mechanics of Deformed body

B



Tenna - 1012willi - to-pul micro - 10-6 M Mano - 10 1/1 pica - 10-10p

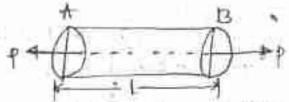
ude

30

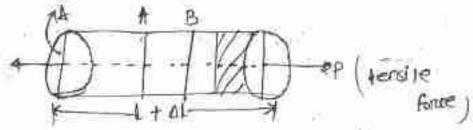
Simple Sheet and strain .

Let us consider a bar of length () and having cleaned of "A" and a tensite knowl of p is being its Longitudinal anis.

En # 3120



force (tensile). The Length of bore is increased to Ac



Consider two Fibres 11' and B'

the state of the s To the look

Tensile Ance) Resisting Ance

Resisting force. freeste

Tensile Striess (T) = Tensile face
Anno

= <u>1</u>

In or booky when subjected to two good and apposite pushed. As a result of which There is a decrease in Length of the booky. Is known as Compressive stress.

compressive stressive)

E Compressive way

Anea

Compressive way

Shear stress - The stress induced in a body, when subjected to two equal and opposite forces which one acting and opposite forces which one acting section. As a neguli of which the body tend to shear off earness the section is known as shear stress.

(T)

ज्ञा कर्म

of Hh

127.15 6 1 35 When a body is subjected to sum e Sexteen extennal face. There is change in dimension of the body. er The notion of change in demension of the body to the estiginal dimension is known as strain change in dimension * Mathmotically & = oniginal dimension There one foure type of strain: 1 Languatinal strain U Lateral Strain (m) volumetric strate (14) Shear Hrain (1) Longitudinal Stanin - It is the rail o be n change in Length to Et's original hangth some Se harrige longitudinal Stool n = 4 = change in lengths ostginal rength The unit of longitudinal statal is unitless Quantity. Laterary strain application of defourning fine is one direction negals in change in passemeders indinection perpendicular

10 11

Consider acquired howing its one and Arra manighed support tex force to is applied. ad 41s her end indown constal direction. > The tength of cylinder small inchease while it's diameter & will decorrose. > Lateral strains The nation between change to its original diameter when the cryphagen is subjected to Se more at " Charle of the even It is defined as the natio bath change in volume. He's orthinal volume * modernatically = U-V = volcement c strain consider about howing a volume vi compressed to a position thoun in the # the 1 v-1c @ shear Strain !- Let ABCO be the choss sectional velw of cube having 1415 Lowert face AB Is freed. > Apply a face stronge tangentially to the opposi face The cube get de Stoned to the poster in ABL D lingle & turned by the lene a shear stoutn is measured by angle by a line orginally payendl. Lucianzo - cular to the timed force tang = DD p Ksmall Lang = 0 Shear Straice (9) = 001 = Displacement Inplane CO Displacement of Plane Co from fixed places

Skrigerien

best displacement le one plane to its displacement le one plane to its

can be determined on observed by the application of Mechanical fince on energy.

direct physical and all that is called as mechanical force which requires to called as mechanical force where are the following mechanical pagents as following mechanical

moderial by windue of which it returns book its original position shedd after nemoval or external , force this known as Elasticity booky.

700 2020

which can sustain without failure:

Followe - 1

Dese to plastic defiamelian permanent noptune

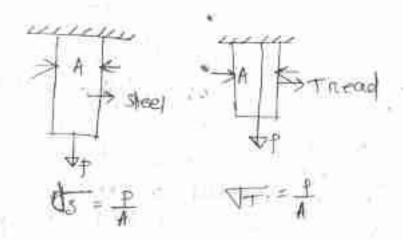
front une

BRIATE medal)

nod > ductile moterial chalk > 3 mille moderial 5-15 / dangation > Intern

5-15 / dangation > Intermediate duette.
>15/ elongation > Completity duetile

Stress doesn't depend upon the material.



Fos = Strength Foilure stress

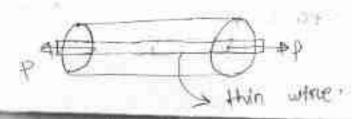
@ esignstress permissible

stress

* Olmension or unitless quantity

(3) Duch lity and battle ness:

of modernou by virtue of which can drown into thin wine.



3.4

0.00

maderial by vintue of which a maderial will undergo how degree of definimation before fracture:

**Due to bottleness **

**Due

(4) Malle abothity: - It is the property of material by Ulatie of which can drawn into thin sheet.

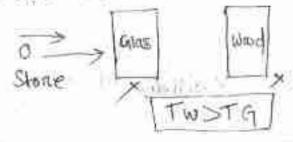
thin wine.

Bue to marreability

O of sange reduction in cisana.

(1) High degree of Plastic deformation.

(3) Toughess: It is the property of material by vinture of which a material absorbs maximum amount of energy before fracture.



Resilience and post nesilience

Strout energy (v): - The energy

Stoned in a body due to deformati-

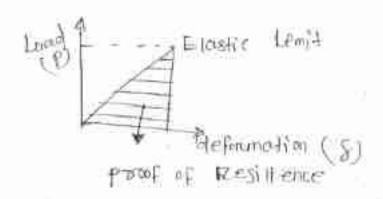
stress bire stress inimize

0

y)

strain energy (y) = Work done due to dasy - Lagemen Load for Strain energy (4) O Greatial lead (11) Sudden load (11) Impact load Laad plastic defirmation > × deformation Strictly energy = 12x37P 161 Resilbence:-The energy absenced by a companient within exastic compt is colled as nesilpence. plostic deformation Resilience desiremention Prest nestience:-Anea under

Proof resilience. Anea under under to existic limite is called as proof resilience.



(7) Stiffness: + SH Is the property of moterial by vintue of which a material nesist deformation is known as stiffness:

1mm 4 100 KN 100 KN = 1 m·m

2mm 4 2·00 KN 2·00 KN = 1 m·m

(SB > SA)

- madestal by virtue of which a madest al lends to deform per manently.
 - (9) Handness gt is the nesistance againer
 - (b) <u>Creep</u> = gt is the Property due to which a material deformation continiously action of a dead load (constant stress) at an elevated a constant temp.

also in the r

Hooks '- Bours

In states that within elastic Limit - The stress is directly) proportional to stroin.

Mathmetically Stress of strain

>> Stress = 0 Strain

where a -> Propertionality Constant
is called as modernes of

> 0 = Stress Classicity.

According to moderne of elasticity is divided ento 3 tants

(a) Young's modules (E)

(c, of, a)

between tensile stress to the tensile
stress on compressive stress to
Compressive strain.

* 9+ 15 denoted by E $E = \frac{\sqrt{1}}{E}$

(b) Modulus of orgidity:- It is the roution bein shear stress (y) to the shear stress (y) to the shear

```
Et es denoted by (CINIG)
                        C, NIGH = Y = Shean strain
He.
DOX-
             Bulk mediation of Emily 19 - ( R)
                     It is defined as the route of
               rustimal stress (TN) to the volumetric
             · Stram.
encion!
              * It is denoted by ( K)
OF
                        K = NN = Normal Stress

Vorumetric strain
            Young's modulus - (E)
                  and I ungetudenal stress to andout
                  Long Audenal Straffi -
                  E = Longitudinal Strain
             The value of E fore different moterial
#o
ile
                     (1) - steel -> = 200 to 220 9p0
                                  =(20040220)2003 N/mm
0
                                  - 20010220) Gu/m2
       (1) Wrought IRAN-E = (190 + 200) Gpa.
                   (3) Cast inon-E = (18040160) Gipa
                    (4) Copper-E = (90-110) Gipa
       (5) Brass- E = (80 = 90) Gpa.
2110
            (6) Wood-E = 10GIPa
DESCH!
                      342 A 1
        PATE S
```

Des remarkant erry body die in Bain Betterpoor

Consider a booky Subjected to All the body I sength of the body

A > Creass sectional 1

anea of the body

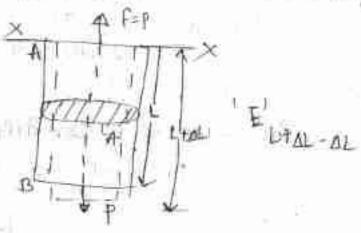
V > Stress induced in the body

(LTA)

E -> Modernes of e both city for the moderator of the body.

E> strain in the body

Al > Deformation of the body



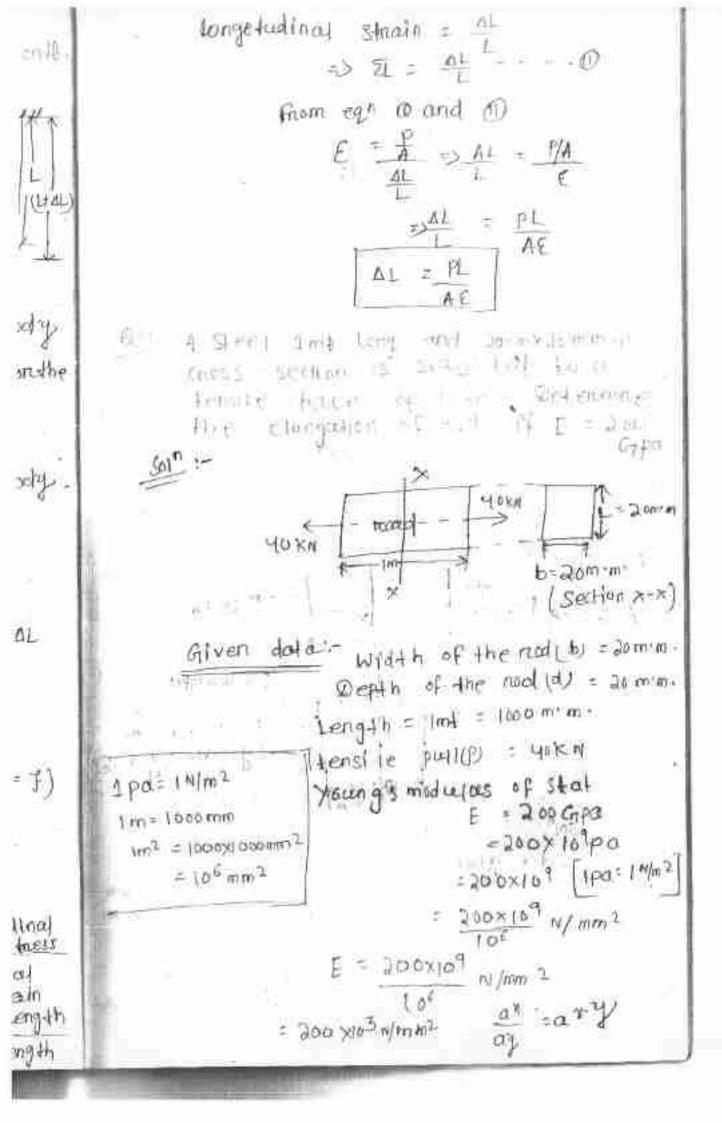
Stress T = Resisting fonce (P=F)

 $\nabla = \frac{1}{A} = \frac{P}{A}$

Young's modulus E = Largitudinal stress

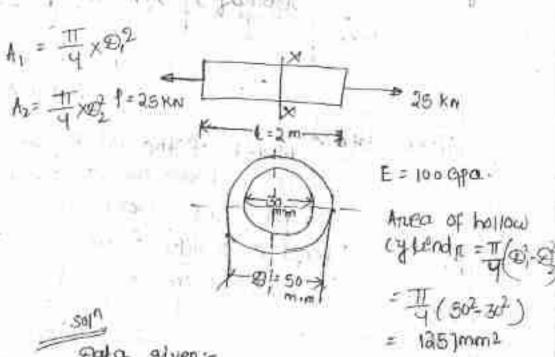
longitudinal Strain

Longitudinal stoom = Change in length



10 John A unique Biry

QUE A honor callendar and long has an diameter form and raide distribution of the standard of consigrity a lead in 19 on find the Striks on the eyunder of the valued modulus of elegants of the charder in the Englanders



Data given:-

Length of the correction = 2m.

Load = 25KN = 28×103 N = 200m·m.

outer dia of cyalloder (81) = 50 m·m· Innen dea of cylender (D2) = 30mim.

Modulus of epsticity =(E) = 1000/pa = 100×100 470 1 PO = 1 m /m2 100 GPQ = 100 × 109 M/m2 · Im = 1000 min 1m2 = 106 mm2 100 GPa = 100 × 109 N/mm2 100 Gpa = 100 × 109-6 NJmm2 = 100 × 102 n/mm2 striess(o) = Resisting face An 100 Resisting force = applied load = 25×103 = 19.8801/mm2 13,57 = 25×16×2000 =0397mm 1257 ×100×165 The elangration on hollow cylinder is 6.397 mm - x 1 Q3 Two wines one of steel and other topper ones a some single and one subsected to same bersion if the diameter of copper wine is some find the dra of steel when & amounted the char of Shee while they and compated by the Same amount, take Esteel = 20 miles.

ï

7

)W

Ċ

: Dw:

auntur. Wi E restent . The clear.

Acec

Acec

Polc

$$x \times 2^{2} \times 100 \times 10^{3}$$

ALS = ALC =(AL)

 $\Delta L = \frac{f'sls}{x_{1}(ds') \times 200 \times 10^{3}}$

$$\frac{Pols}{45! \times 300 \times 10^{3}} = \frac{Plo}{45! \times 300 \times 10^{3}}$$

$$\frac{Pl}{45! \times 300} = \frac{Pl}{2! \times 100}$$

$$\frac{ds}{45! \times 300} = \frac{Pl}{2! \times 100}$$

$$\frac{ds}{45! \times 300} = \frac{4 \times 100}{200}$$

$$\frac{ds}{200} = \frac{4 \times 100}{200} = 3$$

$$\frac{ds}{200} = 3$$

$$\frac{ds}{200} = 3$$

12 oct 2020

Consider a bar AB haviging freely and en

Let L -> Length of the base.

A -> Anex of cls of the ban

E -> youngs modulus of elosticity

w -> sp . wt I will cut of the motorious

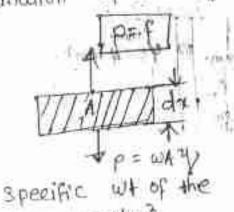
43 = 4

DORGE

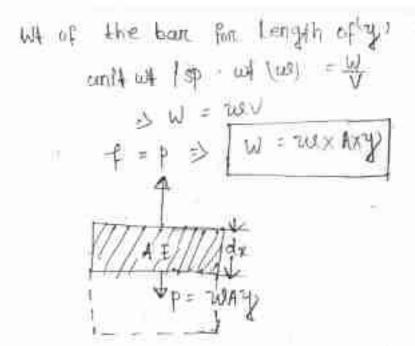
modium

Now consider or smallstrip dir along the length of the barr of a distance of the barr of a distance

Deforemation of a body due to self witi-



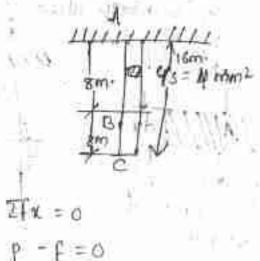
specific whof the material we nulm3



Elongration of the small strip dus to the

: 11 1 年 年 計 章

A steel wine 16 m lang having cls
attent of ulminate weights 20 miles shown
in figure of the modulus of elasticity
(Es) for the wine more and (3200 upo



April 1 may 1

To suffity the condition and ion of equilibrium of equilibrium. The desisting face will be equal margifuede but opposite althorition

40g 12g + 12g - 크리 - 프로젝트 [변화 11gs

2F1=6 2 Fy=0 : 2 Mz = 6

Given data

Total longth of the wine= 16m. CICOLEGE YI 34m-m2, what the wine wis 200 = 200 = 160 cm · m. modulus of elasticity (E) = 200 Gpa = 200 x16 9po = 206×109 m/m2 3 200× 10/4-6) W/mm2

E=200 x 100 11 mm2

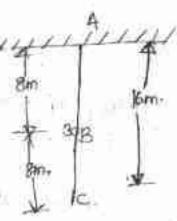
Performation of c'

Clongation due to self wh al = wh - 20× 16 ×105

5×4× 300×103

z 0 . 2m m .

A =4mm2 E = 2007/16 2 mm 2 W = 20 = 10N



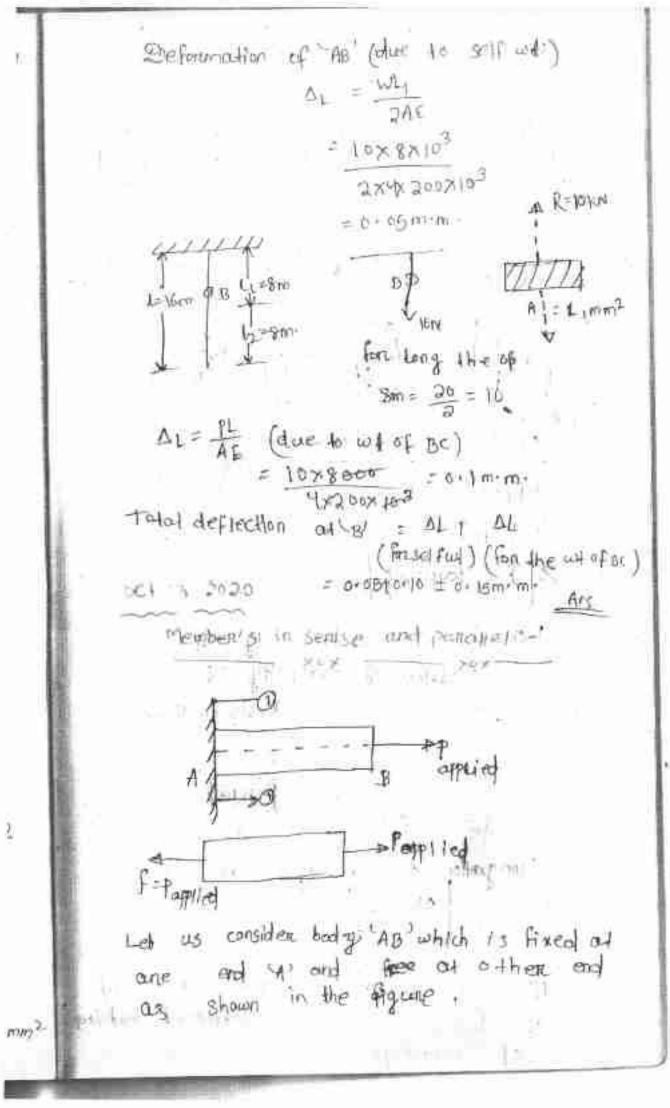
E = 200× 103 m/mm 2

$$L_{1} = 2m \cdot \int_{C} \frac{d^{2} + 1}{c} = 16m$$

$$L_{2} = 2m \cdot \int_{C} \frac{d^{2} + 1}{c} = 16m$$

$$L_{3} = 1/2 \cdot 1A \cdot 24mm^{2}$$

$$U_{3} = 20m \cdot 1$$



Let p be the applied force outling on it (fines and). A lettle consideration well see that if we increate the the applied force (P) Then the mesisting bour will increase of wi The fines body diagram of the body of flied Resisting fince) section Z11=0 Zf1=0 2M2=0 >> Papplied - f = 0" Papplied Let the c1s of the body = 4 Modules of ebsticity . I Resisting force Striess (T Anea - 12 Tro Popplad n Life of to agrai was Elongation due AL = One bons 150 connected and to and of different bength & different miskylug ebalicityMember In Sevise T

- 1 End to end connection
- (a) Load is same in all the members if a single Load is applied and its extreme end

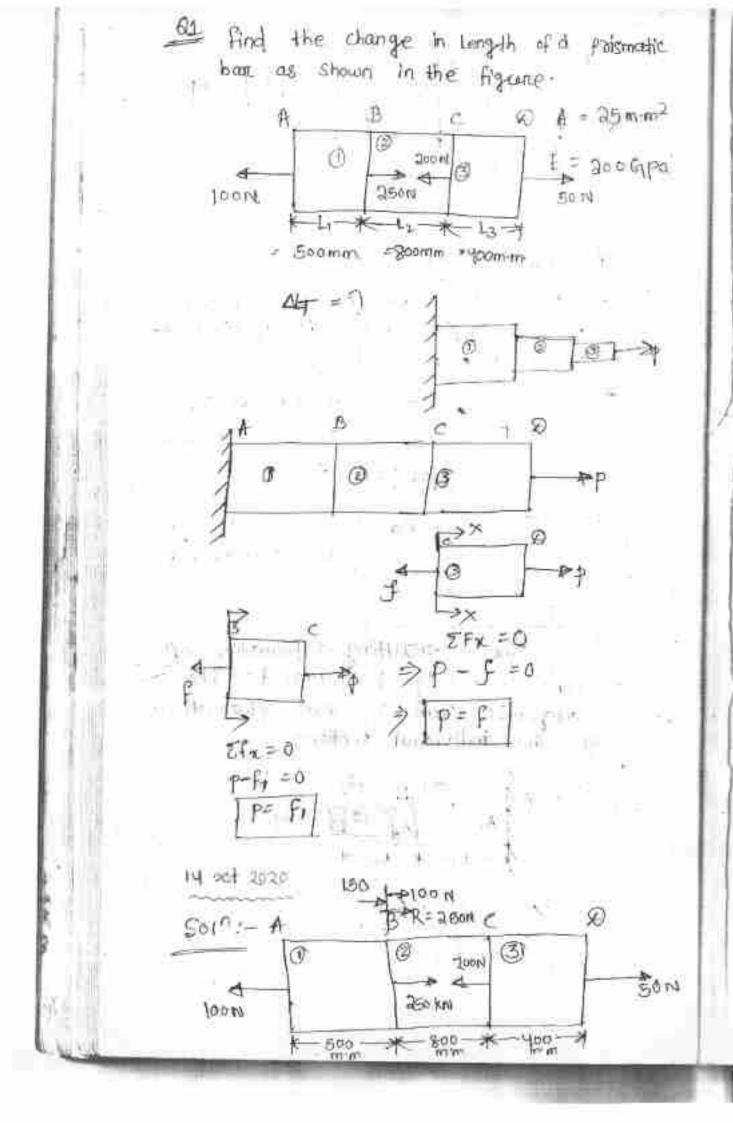
Principle of Superaposition -

Composite budy is equal to the expedic sum of the deformation of the deformation of the individual section.

$$A_{1} = AL_{1} + AL_{2}$$

$$= P AE_{1} + AE_{2}$$

lug



Iooch

L1

B

Compressive

(F) From Poon

(Extension)

(Extension)

(Compressive)

A =
$$\frac{13}{50m^2}$$

Extension)

Given deata:

A = $\frac{35}{50m^2}$

Extension)

Given deata:

A = $\frac{35}{50m^2}$

Extension)

A = $\frac{300 \text{ Gpo}_1}{13}$

Extension)

From Extension

A = $\frac{300 \text{ Gpo}_1}{13}$

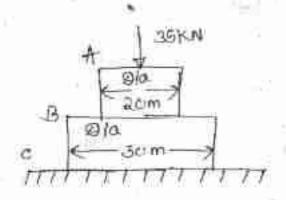
ME

= 1 25×200× 103 (100×500)-(150×800)+(50×400)

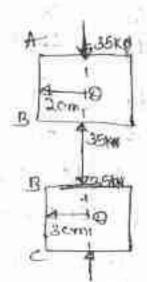
ALT = +0.01mm (Composite)

-ve singn indicate the ban is subjected to compaessive .

A stepped ban as shown in the figure is subjected to an arrivality applied to an arrivality applied to and of 35 km. Find the marrimum and minimum stress developed.



16 oct 2020



Stress (T) = Resisting Rice (F)

mea

Resisting is equal to applied force

$$F = F \quad p > (applied) \quad fince$$

$$Anea$$

$$T < Papplied$$

$$Anea$$

$$T < Papplied$$

$$T = 22.7$$

$$Dia \quad of \quad ban \quad AB' = (du \quad 2cm = 2cm m)$$

$$Dia \quad of \quad ban \quad AB(A) = \frac{1}{4} \times 2e^{2}$$

$$A_1 = 2270 \text{ mm}^2$$

$$A_1 = 2270 \text{ mm}^2$$

$$A_2 = 5107.5 \text{ mm}^2$$

$$A_1 < A_2$$
So $AB \quad is subjected for max^m 3 tness where as born is c. Is subjected to min^m stress.

$$TAB = \frac{35c \cdot 10^3}{Anea} = \frac{F_1}{A_1}$$

$$TAB = \frac{35c \cdot 10^3}{2278} = 15.48 \text{ mi/mm}^2$$

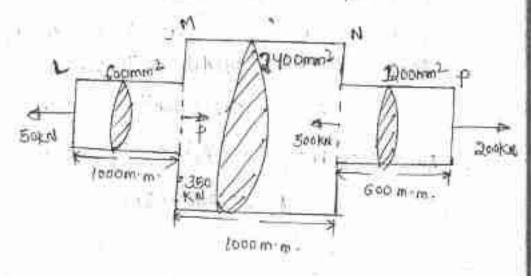
$$TBC = \frac{1}{42} = \frac{35c \cdot 10^3}{42} = \frac{1}{42} = \frac{1}{42}$$

$$= \frac{35c \cdot 10^3}{5107.5} = 6.857 \text{ ni/mm}^2$$$

J mos (AB) = 15 + 48 m /mm²
J min (BC) = 6 + 852 n /mm²
Ans

A member LMNP is subjected to as shown in the figure calculate U.J. force necessary for equilibrium

U.J. Take E: 200 Gm Imil.



UNIT TO BE TO THE STATE OF THE

SOL

Condition of equillibration.

If x = 0

If y = 0

EMz = 0

Total Right word fine in x direction = Total Left would fince in a -direction

>P+200 kN = 500 KN + 50KM

>> Pt200KN = 550km

P = 550KN - 200KN = 350KN

```
Total crongration in composite box
    = ALT = E [ALITAL2 ... ALA]
            (A cconding to painciple of super
                      position)
19 00+ 2020
S1<1) - 1
Pata given 1-
       Anco of segement () = (A) = 600 mm2
       Arrea of segement @ = ($2) = 24 00 mm?
        Anea of Segement (3=(A) = 1200mm2
   Length of Segement () = (Li) = 1000m·m.
   Length of Segement @= (12)= 1000 mm.
    Length of segement (3 = (43) = 600 mm.
    E for the all the segement
                      = 200 Gn 1m2
                     = 200×109 N/m2
                    1m2 = 1000 × 1000 mm2
                         O mm Person
      E = 200 × 109 N 0 93 =0x-8
               1.5 6 m· m²
               200× 10(9-6) N/mm2
             = 200 × 103 N 1mm2.
     ALT = 2 DLITAL2 - Un
```

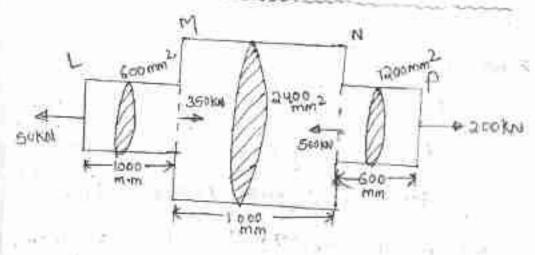
KX.

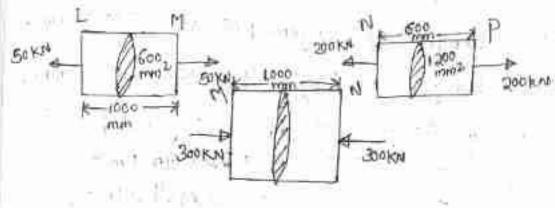
Sn

$$\Rightarrow \Delta L_T = \left[\Delta L_1 \dagger \Delta L_2 \dagger \Delta L_3 \right]$$

$$\Rightarrow \Delta L_T = \left[\frac{P_1 L_1}{A_1 E} \dagger \cdot \frac{P_2 L_2}{A_2 E} \dagger \frac{P_3 L_3}{A_3 E} \right]$$

Step-11 F-B-D of different section





Load on segment $\mathbb{O}(P_1) = 50 \text{km} = 50 \text{km}^3 \text{N}$ Load on segment $\mathbb{O}(P_2) = 300 \text{km} = 300 \times 10^3 \text{m}$ Load on segment $\mathbb{O}(P_3) = 200 \text{km} = 200 \times 10^3 \text{N}$

- The appared load is shared among the members [w=wctws].
- > Definition of each member will be equal $8f_1 = 8b_2$

20 oct 2020

Analysis of bass of composite section-

Comment of the second

> A composite bare many be defined as the bare is made tup of two for more different materials. Joined trayather.

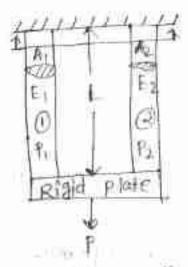
MADE THE SHIP TO BE T

- > for composite bout the following two points one important . ..
 - 1 the extension on compression is equal

The total external Load on the Composite box is equal to the sum of the Loads consided by each difference of the modernal w= WITWD.

> consider a composite bour made up of two different materials. tel p-rotal load on composite bon L -> Length of Composite ban and also lengths

of bans of different



A1 & A2 -> C1s area of bon 10 and 10 nespectives.

E1 & F2 > yeargls modulus of hom @ and @

P1 & P2 -> Load staned by ban (and ()

TI & TE Is stress induced in bon @ and bor O nespectively.

Total load (P) = P1 + P2 (on composite p = PITP2

Struess in barro = Pi > TI = PI > PI TIAI

Similarity stress bor @(T2) = B2 = T2AL Put ex 10 x 10 in eqn 0 In member @ > Strain to member I P = PITP2 = TIA, TEDAQ.

P = OTA, + T2/AQ 1 1

Stock in member 1 = Strain to mentock II

El en (modular netion)

nt

21

m Ffen A neinforced concrete column socials of con in section is relinforced with 4 nos of steel boar of dia 2.50 on one in each comer. The column is constraint a lead 200 tones - fried the stress in concrete and steel Plake Es - 2 1x10 kg/cm2.

Be = 01/4x10 c.kg/cm2

Dotagiven :-

Total load on column = 200 kmom

(P) = 200 × 103 kg/

(Is oned of the column of 400 s 2.5cm.

Ag (gnoss Arrea) = 500 cm/50

c/s area of Steel=4x=4x=4xd2

C/C knee of concrete = Ay -As

Ac = 2500 - 19.634

= 2480 · 366 cm2

Total load = Local on steel + load on concrete

P= Pst Pa

=) P= JSAN TOAM.

= > 200×103 = - T3×19.634+TC ×12480.366

(1) Strain in steel = Strain in Concaste $\frac{\sqrt{3}}{E_{S}} = \frac{\sqrt{2}}{E_{C}}$

VS + Es To Es = 2.1 × 100 kg/cm2 0.14×106 Kg/cm2 \$ T3 = 15TC Put the value of eq (1) in eq " (1) => 200× 103 = 15TE (19:634) + TE (2480 +366) > VE = 72 Kg /cm2 1 Vs = 15Vc = 15×72 = 1080 kg/cm2 21 oct 2020 rutgled bar ABCD is hinged at you and supported in a fortizontal position by two identical steel wines as shown in figure . A ventical Load of 30 km es applied at 13, And the tensile forces Ti and Tz induce in the wines by ventical local Ti d Int 4To 81 -- tmf --

7

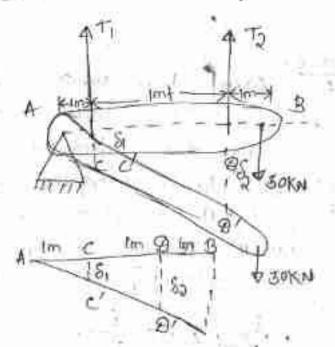
356

Regid box means the box which remain

Two Identical steel whites means the anea of cross-section, length and the value of E' for both the white are same.

(A1=A2) (1= (2 =1 (1m) E1= 5

F-8.9



Tibe the tension in the first were.

The bethe tension in the 2nd were.

So be entension of the first were.

So be extension of the 2nd were.

ΔACC and ΔADD'

ΔACC ≅ ΔΑDD'

$$\Rightarrow \frac{S_1}{S_2} = \frac{1}{3}$$

$$\Rightarrow \frac{S_2}{S_2} = \frac{1}{3}$$

$$\Rightarrow \frac{S_1}{S_2} = \frac{P_1L}{A_1E_1}, \quad S_2 = \frac{P_2L}{A_2E_2}$$

$$PUH \quad \text{the values of } S_1 \otimes S_2 \quad \text{in egn} \quad 0$$

$$\Rightarrow \frac{P_2L}{A_2E_2} = 2 \times \left[\frac{P_1L_1}{A_1E_1}\right]$$

$$\Rightarrow \frac{T_2L}{A_2E_2} = 2 \times \left[\frac{P_1L_1}{A_1E_1}\right]$$

$$\Rightarrow \frac{T_3L}{A_2E_2} = 2 \times \left[\frac{T_1L}{A_1E_1}\right]$$

$$\Rightarrow \frac{P_3L}{A_1E_1} = 2 \times \left[\frac{P_3L}{A_1E_1}\right]$$

$$\Rightarrow \frac{P_3L}{A_1E_1} = 2 \times \left[\frac{P_3L}{A_1$$

T1 = 18KN , T2 = 36 KN Ans

3 NAV 2020 -

Problem-1

A square but of 20 m side is held between how raigid pintes and Landed by an addat force of p' equal to 30 tonnes as shown in the figure first the neactions at the ends 1/2 and 1/2 and the extension of the partion 1/18 Take

Jem Lacim

Solde of the bar (a) = 2 cm.

Force on the bar (p) = 30 ton

-30×103kg/

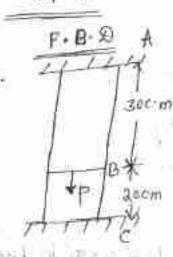
Length of bar (AB) Lab = 30cm.

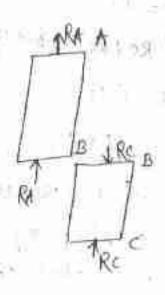
Length of bar (BC) Lac = 20cm

Youngs modulies (E) = 2×106kg/cm²

Area of the bar = 02 = 22cm=4cm²

34p-(11)





RATRC = P

Step - viii)

RATRE = P - 1

RA + Rc = 30×103 kg - 0

Elongation in box AB = Compression in the box BC.

> ALAB = ALBC

AABE PAGLAGE

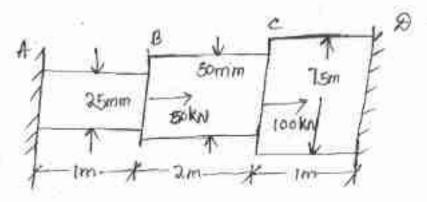
1-44

Problem -2

A criculant steel bor ABCD

ruigidity fixed with of A' and B' is
subjected to axial boads of so kn and
lookn at B' and c' as shown in the
figure find the boads shared by each
part of the bar and the displacement
of the points B' and c' Take "Es' =

207 kn 1mm²

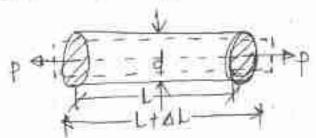


4 nove 2020

A LON 3050

Podson's Ratio -

It is defined as the natio of lateral strain to longitudinal strain.



Mathmetically:-

ru = Lateral Strain Longitudinal Strain

= AB (concutary) Ad on B (nectargle

4

> Laterial strain : rextanglitudenay strail

> The value of 1 variles from 0, 25

> It is a demention less quartery. Problem I Presone the change in Length bureadth and trickers of speci bear which to the long. James buccosth & John Hock and it is subjected to an water pain of 30km in the direction of Pts Length take E = 2×100 N from 2 and poliston Talls 1 1 3 -30mm Qada given !-Length of the bancles = 4m. width of the ban (b) = 30mm Thickness of the ban (t) = Jomm. Andal pull (P) = 36KN / 36×103KN Young's modulus (E) = 2x 105 N/mm2 poissonis radio(10) = 0.3 Anea of cross section (1) = 30 mm x 20mm - (00 mm2 re = Lateral Strain Longitudinal strain > re = $\frac{4b}{b}$ and $\frac{4}{4}$

AL

$$= \Delta L = \frac{PL}{AE}$$

STEP -11 Change in Length

$$\Delta L = \frac{FL}{AE}$$

$$= 30 \times 10^{3} \times 4000$$

$$600 \times 3 \times 10^{5} \, \text{N from}$$

$$\Delta L = 100 \, \text{mm}$$

Hockes Law-It states that within elastic Lemet stress es dénectify propertions -L to the strain. Mathmellcally stress of strain Young's modeling stress = constant xstrain modulus of Constant : Stress Strain BLAK modulus of elasticity Young's modulus(E) tensile stress of compressive densite strain or compressle Strah E- = 4M longitudinal and lateral Strain Modules of regidity (c, on Gor N > It is the note bett shear stress to shear steam. It is denoted by c, N on G. Mathematically (G)

But Godalus (K) :-

> It is the natio bet more stress and volumetric strain.

> et es denoted by ki

> cloutimeticoully k = Norumani stress - volumetric stress

(TIL = TY = TZ = T) > bulk EVS truss.

> St es the natio bear change in volume to Pais ordiginal volume.

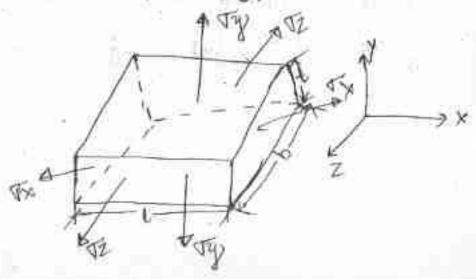
> It is denoted by evonev

> Mathmetically Ev = AV

AV = Final volume - Inteal volume

Inetial volume

Subjected to three mutually perpendicularing for forcess of stress:

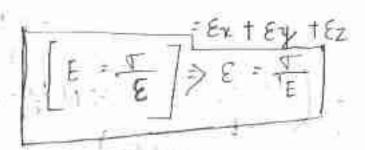


Consider a meetingular body subjected to direct tensile stresses (tve) alongy three perpendicular andces as shown in the fig.

Let $\nabla x \to \text{poission}$ Ratio.

Let $\nabla x \to \text{stress}$ in x-x direction. $\nabla y \to \text{stress}$ in x-y direction. $\nabla z \to \text{stress}$ in z-z direction.

Volumetric strain (EV) (ifseton V)



Strain in x-x direction $E_{x} = \overline{T_{x}}$ Strain in y-y direction $E_{y} = \overline{T_{y}}$ E

Strain in z-z direction $E_{z} = \overline{T_{z}}$

A lettle consideration will take that when the stress applied direction is subjected to elongation where as The apposite two direction subjected to Compression.

$$\mathcal{E}_{V} = \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} = 0$$

$$\mathcal{E}_{V} = \frac{1}{4} \frac{1}{$$

```
Frakiem - I
```

A steel box 2m Long Jumin winto are 15 mm thick is subjected to a busine to aid of 30 km finel increase in volume is plissin's nearly (1)

and Jeung's modulus(E) = 200 Gipa

Ev = TI + TY + TI (1-2 ml)

Ev = TI + TY + TI (1-2 ml)

Ev = TI (1-2 ml) contactal.

Soll

Data given:

Length of Steel bar (1) = 2m.

Width (b) = 20 mm

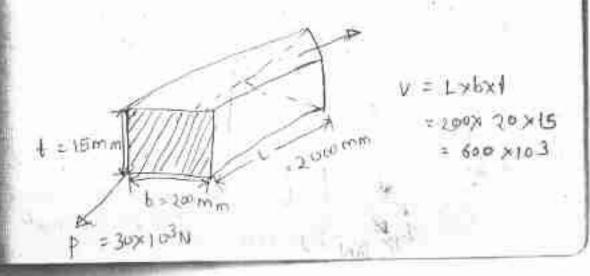
Thickness (t) = 15m.m

Tensite lead (p) = 10 kN

poisson's ratio (Ne) = 0.25

Though younges moderlus (E) = 200 Gpa

= 2000 (p) N/mm².



$$E_{V} = \frac{\sqrt{4}}{E} \frac{1 \cdot 2\pi}{1 \cdot 2\pi}$$

$$E_{V} = \frac{P}{E} \frac{1 \cdot 2\pi}{1 \cdot 2\pi}$$

$$= \frac{P}{btE} \frac{1 \cdot 2\pi}{1 \cdot 2\pi}$$

$$= \frac{P}{btE} \frac{1 \cdot 2\pi}{1 \cdot 2\pi}$$

$$= \frac{30 \times 10^{3}}{20 \times 15 \times 200 \times 10^{3}} \frac{1 \cdot 2 \times 0.25}{1 \cdot 2 \times 0.25}$$

$$= 0.00025$$

$$E_{V} = \frac{\Delta V}{V} \Rightarrow \frac{\Delta V}{V} = 0.00025 \times V$$

$$= 0.00025 \times (600 \times 10^{3})$$

Problem - 2

A Steel Hinck: Cube of somm

wich e is subjected to a forte of 6

kni (Mensite) 8km (compare ssion) chici yen

tensite) along he y and 2 direction

nespectively betermine the change in

without of the block take i = 200km/

mm - and m = 15

Sall:- $P_{N} = 6 \mu v$ $P_{N} = 6 \mu v$

```
Step-I
     sade of the cube (a) = 50mm.
     Fonce in 1-x direction = (92) = GKN
                      = 6×10<sup>3</sup>N (Tensila)
     Force in y - y direction (py) = 8km
                              = 8×105N
                                  compressive)
    Force in z- Z direction (Pz) = 4kn:4x103 M
                                  (Tensite)
      E = 200 KN /mm2 = 200×105 N/mm2
   m = 10
   change in volume (AV)
                = (TI + TI) + TZ ) (1-2 NR) XV
step - II ordanal votume of steel cube
       = 503 = 125 × 103mm3.
   stress in x-x dinection
            Viz = Px = 6×1.03 = 2.4 N/mm2
    stress in y-y direction
          Ty = Py = 9x103 = 3.2 N/mm2
     stress in z-z direction
              VZ = PZ = 4×103 = 1.6 N/mm 2
               M 50x50
```

3

B.FV

: Hill

117

KL J

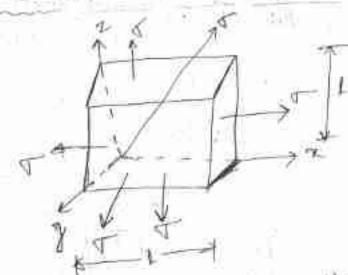
1 4110/2035 Step. III strain in n-x dineation - Tx - MIF - NTE $=\frac{2.4}{E}-\frac{3.5\times3}{E}-\frac{3}{10}\times\frac{1.6}{E}$ in y-zy dimeetlan strain Egy = Ty - x Tx -x = $=\frac{-3.9}{F}-\frac{3}{10}\times\frac{3.9}{F}-\frac{3}{10}\times\frac{1.6}{F}$ E 2 2 3×214 3×166 $=\frac{1}{E}\left[-3\cdot 2-\frac{3\times 2\cdot 4}{10}-\frac{3\times 1\cdot 6}{10}\right]$ Stanin in Ezz direction 起= 里 - ル 里 - ル (項) = 正一内要十八年170 = 1.6 - 3 × 2.4 + 70× 3.2 E $=\frac{1}{E}\left[1.6-\frac{3\times2.9}{10}+\frac{3\times3.2}{10}\right]$ = = X 1.84 Step-(IV)

Step - (IV) Volumetric Strain EV = Ext EY T EZ

=
$$\frac{3^{\circ}88}{E} - \frac{919}{E} + \frac{1.89}{E}$$

= $\frac{1}{E} \left[\frac{1.89}{E} - 4.94 + 1.89 \right]$
=> $\frac{1}{E} = \frac{0.32}{E}$
= $\frac{1}{E} = \frac{0.32}{E}$
= $\frac{1}{E} = \frac{0.32}{E} = \frac{1.32}{E} = \frac{1.32}{E} = \frac{1.32}{200 \times 10^3}$

young's modulate (E) in



Consider a cube whose sides are 1?

Let the Cube is subjected to thine p

mutual perpoendicular stresses (Tensile)

of equal in tensilary

or the forees

tet > stress or the forees

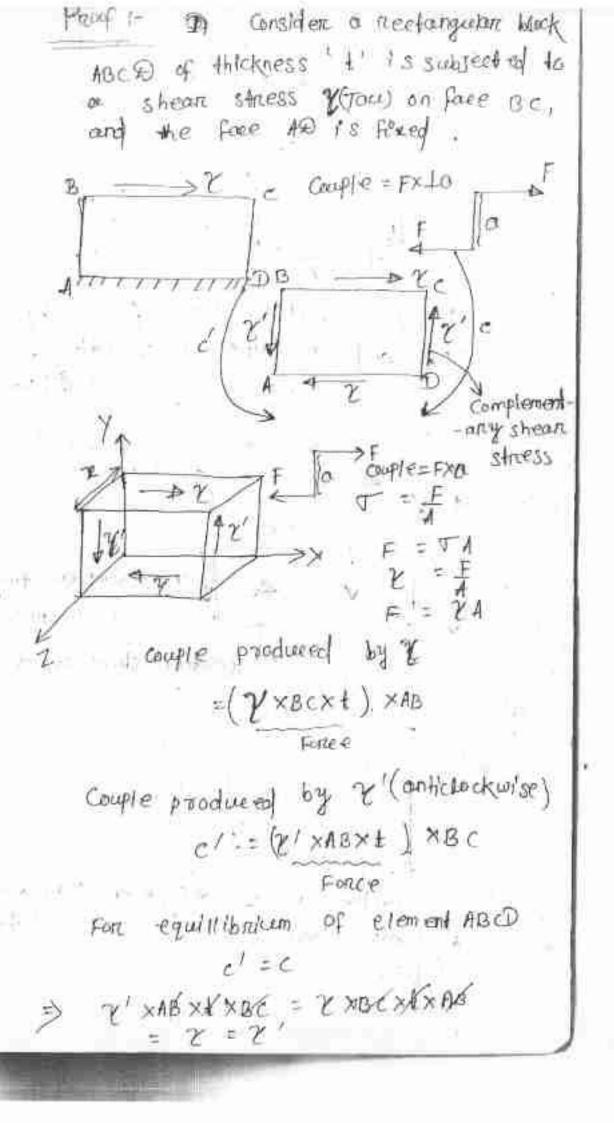
tet > poisson realto

We known that volumetric strain. EV = Ex- Ey - EZ Studia in x x direction THE - ME - NET Steal in y-y direction Ty = I - NI E - MI Strate in 7-1 direction. $\overline{\xi}Z = \frac{1}{T} - M \frac{T}{F} - M \frac{T}{F}$ IN = (= - N= - N=) + (= - x = - N=) + (= -MI - MI) = 3[(1-11) Bulk modulus (K) = Norumal Stress Vojumelnik strain F. 50 亚(1-2/12) タK=長(1-2NU) > [E = 3k (1-2 M)] (v.v.I) H 14 SH

10 MOU 2020

Principle of shear stress :-

across a plane is always accompained by a balancing shear stress a cross the plane and normal to it.



Eventy shear stress is accompained by an equal complementary shear striess. an a plane out right angle. Relation bet modulus of elasticity modernes of rigidity. Complementary shearn stress 2 = Reputive shear striess Consider a cube length LU subjected to shear striess & as shown in the Flyware

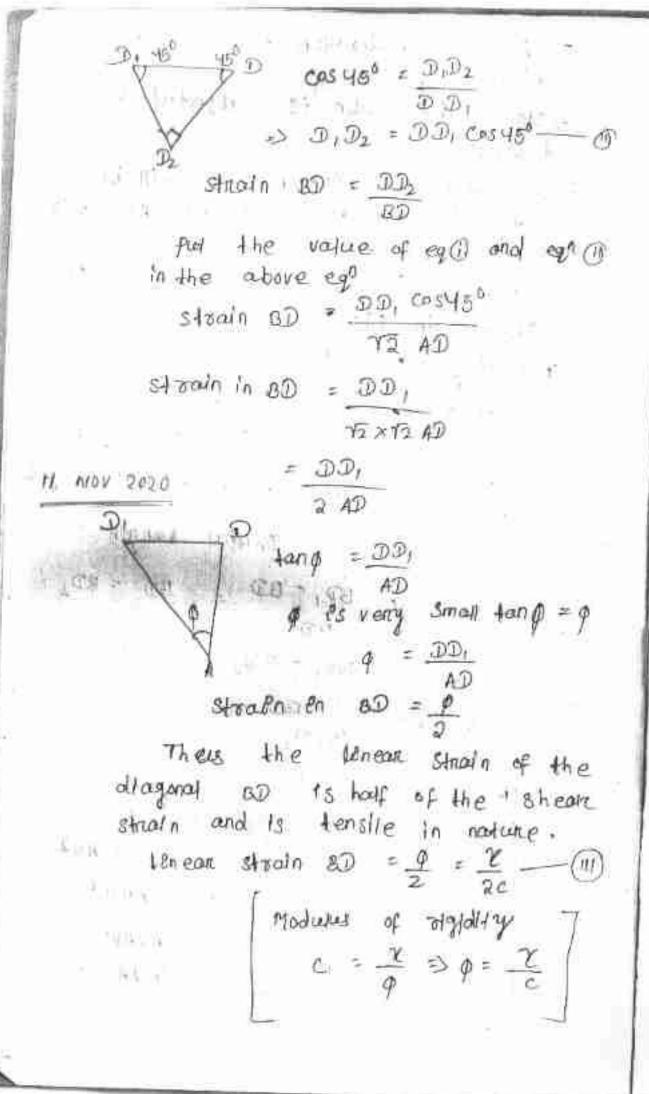
THEORY SUBJECT - Structural Mechanics (TH-1)

? A lettle consideration will show that alse to these > stress the cube is subjected to some distruction . > such that The diagonal BD will be elongated and the diagonal Act will be shoulend -> Let the shear stress & couse the shearstrain (P) The diagonal BD is increased to BD' strain in BD = Change in Length anighnal bength = final Length - Intlat Length Prittal Longth $BD_1 - BD$ $BD = BD_2$ BD _ BD, → BD₂ 30 THE PERSON NEWSFILM SANAT 502 = AD2 TAB2 BD 2 = AD2 + AD2 BD 2 = 1 AD 2 GD 2 = \ 2AD2 -

13

= V DAD -

1)



or -> shear sheas c -> modulus of rigidity. tensile strain on the diagonal BD due to tensile stress on the diagonal 6D = <u>Y</u> tensile strain on the diagonal BD due to compressive stress on the diagonal Ac : re 12 - 10 SO TOTAL STRAIN IN DD = IT + NI TE 57 (11 M) - 0

Compare eqn (iii) and(v)

$$\frac{\gamma}{2c} = \frac{\gamma}{f} (11 \text{ NL})$$

$$\frac{\gamma}{2c} = \frac{\gamma}{f} (11 \text{ NL})$$
Formula

the street of the Land

A, B, C, D, E, F, G, H, J, J B

1E(1-0M) = 29(HIM)=3K (1-2M) E = 29 (1+ M) = 3K (1-2M)

For a given material youngs modules (E) in 120 Gipes a find balk includes band i lateral contraction of a reputed bars of some inclination and 2.5 m. Long when streetched 2.5 m. Take pressons rate as 0.25

K = E 3(1-20m)

BOULK modulus K = B 3(1-2AL)

= 120×163 3(1-2×0:25) = 80×163 N /mm2

= 80 Gpa

ne : longitudinal strain

lateral strain

> Lateral strain = rux lateral strain langitudinal strain

=> Lateral Strain = longiculinal strain

N

Longitudinal strain = $\frac{81}{1} = \frac{2.5}{10.5 \times 10^3}$ = 1 = 0:00] Lateral Strain = 0.001 = 4x10-3 Ad = 4×10-3 => lad = 4x10-3 x50=0.7mm 11 Ans Nov 13 2020 Prob-1 In an experiment, a ban of 50 mm dia is subjected to a pull of GOKN. The measured entention on gauge Length of 200mm isolog min and the change in eliameter is step I peameter of bare (d) = 30m·m· Tenselle. Pull (P) = 60 km = 60 x 103 N Length of specimen (1) = 200 m. Entention in Length (AL) = 0.09m·m. change in diameters (At) = 0, do39 mm Langitualina step-II poisson's Ratio (M) = Longth attal strain Lateral strain 41

Longitudinal strain =
$$\frac{\Delta Q}{200}$$

= 0.009

Loteral strain = $\frac{\Delta Q}{200}$

= 0.0039

= 0.0039
 $\frac{\Delta Q}{30}$

= 0.0039
 $\frac{\Delta Q}{30}$

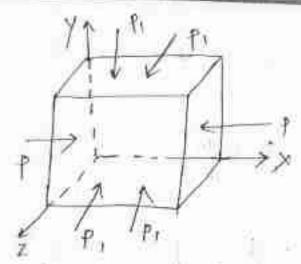
= 0.0095

$$\frac{cu \cdot k \cdot d}{AE} = \frac{pL}{AE} = 3.461$$

$$\frac{d}{d} = \frac{60 \times 10^3 \times 200}{200^3 \times 200}$$

$$= 188552.19$$

A complete block is subject of the completely the completely the completely the completely the completely the apply court of constant completely the apply court of constant completely the apply court of constant completely the constant of constant constan



step-I A cubical black ABCDEFOH and Load on tule opposite faces AEDH and BEGC = p (comprises). The other two faces will be subjected to Noteral tensile Strain. Now in order to pressent the laderal strains other two dimentions. We have to approved a compressive load of present attends of dimention.

Stress and strain curve fortualle and longthe material:

Ductelle Material :-

prosperity that material is called as dualite materials

and the material has large reduction in crossellon and high degree of deformation and and the tensile Local es known as ductivity.

16 Nov 2020

A directly depends upon the 1/2 elongation 1/2 elongation - final length - initial length

In the 1/2 length

XE $\angle 5\%$ \longrightarrow InvHtle material 5% < E% < 15% \rightarrow Intermediate duetile material

E% > 15% -> duetile melerial stress - strain curve of duch'le maderial:-> This lest is penformed by the equerpme
of es called cut m -> universal testing clacking. > It the couchan content 1/ Ps less . That material is called as eluetile modernal (Mild steel) (F2250) Janase Dog bone specimen America of the The cent to the stock of propartional to the stock of propartional AB to B -> Elastic Lemit The body natures back to etsmoriginal position after removal of external force. That Lemit - es called as exastic lemit B to C -> upper yearding, The point at which the maternial strain to yelding.

ibn

h

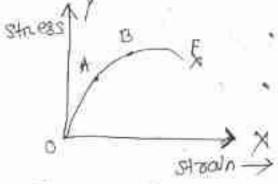
6

c-8 -> Nower Yelld point:-

The point at which the material es achived its mone stress of failure is called as externate point.

D-F > breaking point.

stress - strough Counse of built Lemoutedal:-

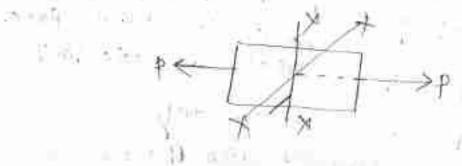


This is the curve of builtle material.

new chapters stress & strains (cenit-4)

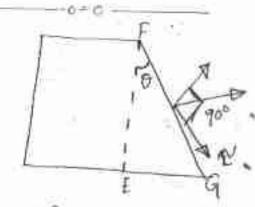
authory on a poincepal plane is called as poincepal stress.

principal plane: The plane which have no shear stress is called as principal plane.



107	Stress = Resisting fixee
ñ	- An.ea
	Mathod of determining stress on abugue
	plane :- (Indine)
	> there are two methods for determ;
11-	1) Analytical Method.
	(1) Grouphical Method.
	Analytical method for deformining stress on obligive plane:
î.	the Pollowing three casses will be considered.
	O'A member is subjected to crular (on) direct striess in one plane.
	Pr. Pr.
	(1) A member es subjected to stress
we	in two mutuality perpendicular direction
	the state of the s
	(111) A members Subjected to shear stress
	1 L Cry

Resultant stress :-



R2 = p2 + 02 + 2p0 cos0

18 = 145 + 15 + 31 N 5 00 2000

TR = VN2 + 22

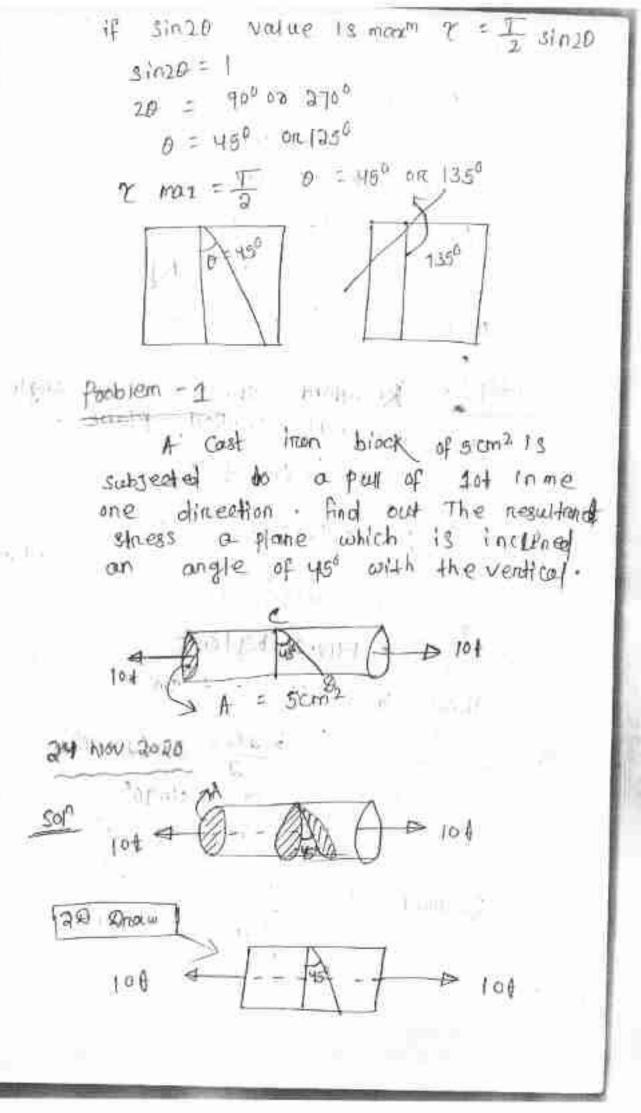
The more stress is more in an inclined plane when cost of or cost of or

VN = VCOS20

when 0 = 0° cost 0 = 1

(TN) manum = T

That means the line FG conclude with the line FE man, tangential stress in an incremed plan when it is subjected to dincet stress in one dincetton



2010 given :-

Anea of cross cetion of cost Erron block $(A) = 5 \, \text{cm}^2$.

Aziai pull (P) = 10+

Angle of obseque plane (0) = 450

step-2 Resultant steess at an angle of 45° with vertical Plane.

 $TN := T\cos^2\theta$, $T = \frac{P}{A} = \frac{10,000}{5}$ $= 2000 \times (03^245^0)$

101 < = 1414.21 kg/cm2

Shear stress (2) = 5 sin20

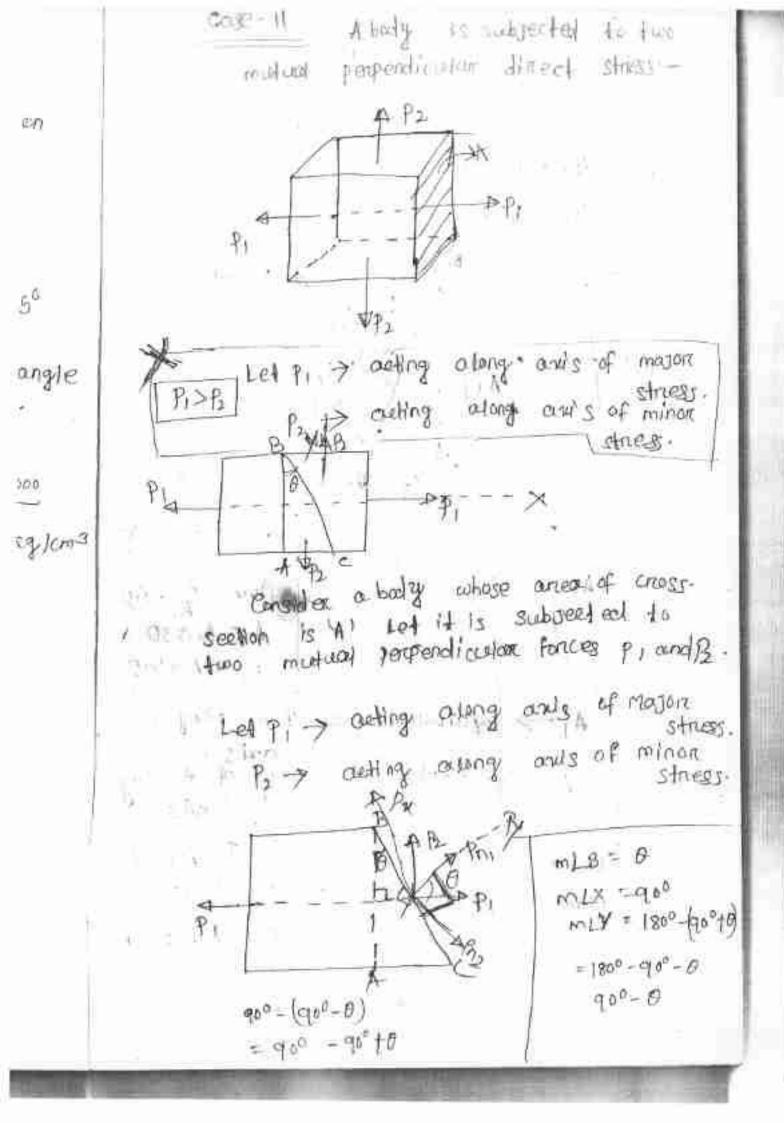
= 2000 sin (2 x 450).

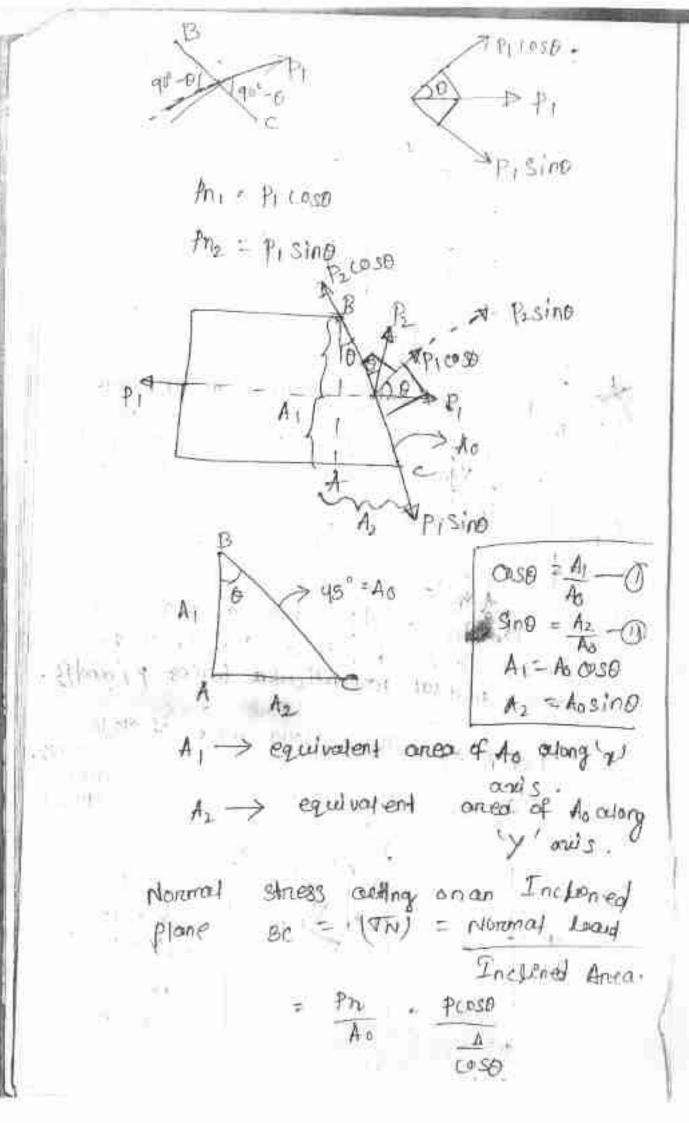
" = 1000 x 210 40"

= 1000 kg/cm2

Regulary stress VR = 1 722 + 22

2 (1414.21) 2 + (1000) 2





$$= \int_{A} \cos^2\theta = \nabla \cos^2\theta$$

$$|\nabla N| = \nabla \cos^2\theta$$

Tangential stress (97) = 7

plane will be mare when cosin when

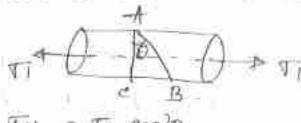
17 33 1 8

ALLO THE RESERVE TO THE PARTY OF THE PARTY O

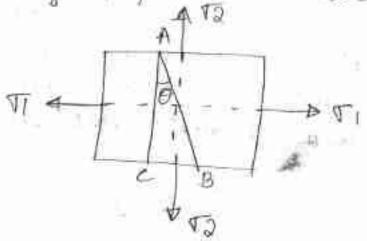
Kt. 60

1

dinect stress in one direction.



When a body is subjected to two mudually perpendicular stresses.



$$\phi = \tan^{-1}\left(\frac{\mathcal{L}}{\sqrt{N}}\right)$$

61 The fensile stress in a point arress for midually perpentir law planes and well from 2 (Fens III) and so refinm 2 tensile) Determine the normal tanga - Hal and nestelland states on a plane at 30 to the ow of the minar AxI s of minor VD = Go N/mm 2 STRESS principal stress 114 A ST = law/mm2 72-60 N/mm2 step-1 Data given: major princepal stress TT = 120 N /mm2 2 425 R W. Tensile) Minor poincepal stress To = GON/mm2 -> angle which the plane with and s of minor chess 0 = 30° poincepay Normal Stress TN = 17+ TO + (57-50) = 120 + 60 + (120-60) cose00

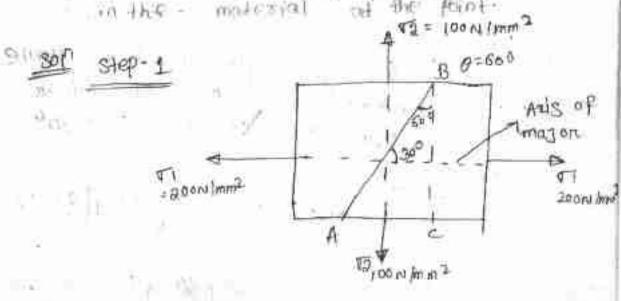
Tangential stress (
$$\mathcal{C}$$
): $\frac{\nabla i + \nabla j}{j} \times \sin j\theta$

$$= \frac{120 - 60}{3} \times \sin(3 \times 30^{6})$$

$$= \frac{130 - 60}{3} \times \sin(3 \times 30^{6})$$

$$= \frac{130 - 60}{3} \times \sin(3 \times 30^{6})$$

(Campassive) - Determine the cases which she major siness had been direction the major siness had been direction to the major siness. Also determine the major siness had been directed to the major siness and direction.



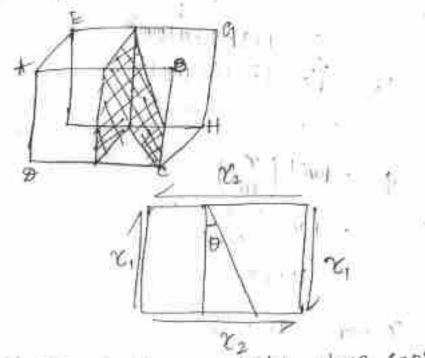
```
step-11 Daya given :-
       majore poincepal stress of = 2000 1mm2
       Minon principal stress To = - 100 11 fmm 2
           0 = 1800 - (90°+30°)
            = 600
Step- III NORMAL STRESS TN = TIT VD + TI - VD COSDO
            = 300-100 + 300-100 CO2 1300
              = 50+150 CUSIDOO.
              = -25 N /mm 2
   Tangential stress (C) = VI - To since
               = 200-(-100) sinido o
          = 129.90 NImm2
    \varphi = \frac{1}{4} \alpha r^{-1} \left( \frac{r}{r_N} \right)
       - tan ( 25
       = 10.89
  7 mar = 17 - 15
  = 200 - (-100) = 150 m 1mm2
       2
```

han

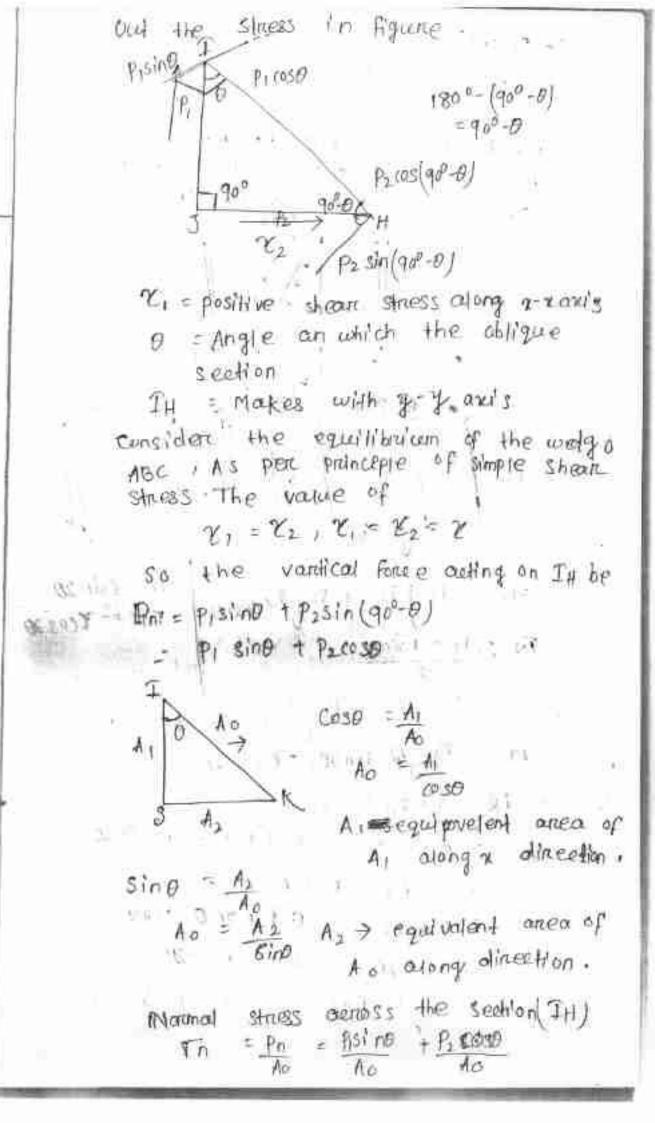
30 A some block is you tong 130m high and 0.50m thick . It is subjected to uniformity distributed tensile forces of the resultants 1200m & Soon as soon in the figure . Corculate, Normal stress and shear stress develop on the diagonal 4 500N 9 000 2020 (AB) -Prove Question 1200N 30

A body is subjected to shear stress.

500N



Let us consider a body whose crossembray ounder 15 41 Let H is subjected to a positive shear stress along a rackly Now Let us consider cen oblique section It inclined with g-y andg on which we are negatined to filling



1

de

8

Short

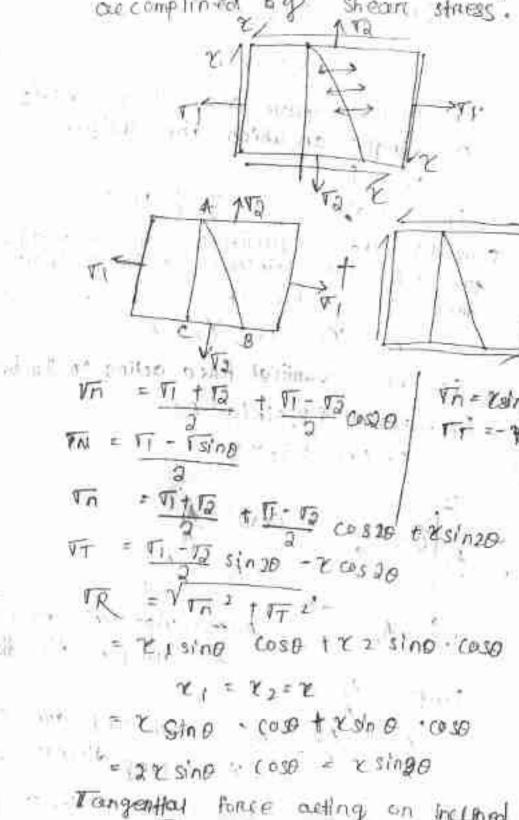
288

mi

$$= \frac{P_1 \sin \theta}{A_1} + \frac{P_2 \cos \theta}{A_2}$$

$$= \frac{A_1}{\cos \theta} + \frac{P_2 \cos \theta}{\sin \theta}$$

A body is subjected to two mutuary perspendicular direct stress and accomplined by shear stress.



Tangentlas force acting on inclined Phone (Thy

- 086

$$P_{T} = P_{2} \cos(qa^{0} - \theta) - P_{1}\cos\theta$$

$$= P_{2}\sin\theta - P_{1}\cos\theta$$

$$\text{Shear Shress aethor on the Inclined plane}$$

$$P_{K} = P_{1}\sin\theta - P_{1}\cos\theta$$

$$P_{K} = P_{2}\sin\theta - P_{1}\cos\theta$$

$$\frac{P_{1}\sin\theta}{P_{2}\sin\theta} - \frac{P_{1}\cos\theta}{P_{1}\cos\theta}$$

$$= Y_{2}\sin^{2}\theta - Y_{1}\cos^{2}\theta$$

$$= Y_{2}\sin^{2}\theta - Y_{1}\cos^{2}\theta$$

$$= Y_{2}\sin^{2}\theta - Y_{2}\cos^{2}\theta$$

$$= -Y(\cos^{2}\theta - \sin^{2}\theta)$$

Principal plane - The plane which have no shear stress . That plane is known as poincipal plane. The stress in the poincepal plane stress.

We known that 2 = 4.

$$\Rightarrow \frac{\sqrt{1-13}}{2} \frac{\sin 2\theta - x \cos 2\theta = 0}{\cos 2\theta}$$

$$\Rightarrow \frac{3 \sin 2\theta}{2} = \frac{x}{\sqrt{1-13}}$$

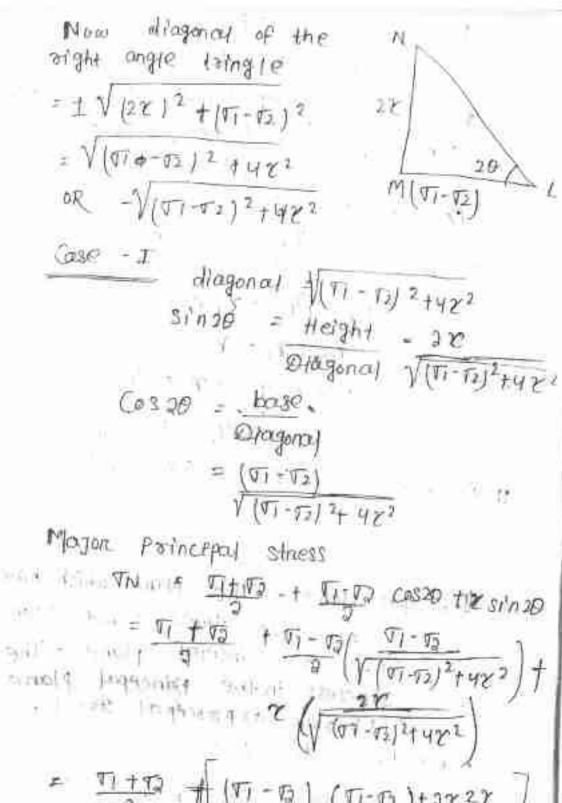
$$\Rightarrow \frac{3 \sin 2\theta}{\cos 2\theta} = \frac{x}{\sqrt{1-13}}$$

$$\Rightarrow \frac{3 \cos 2\theta}{\cos 2\theta} = \frac{3 \cos 2\theta}{\sqrt{1-13}}$$

$$\Rightarrow \frac{3 \cos 2\theta}{\cos 2\theta} = \frac{3 \cos 2\theta}{\sqrt{1-13}}$$

De De

PS 20



Minor poincipal stress :-

1

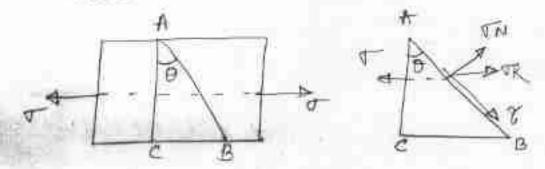
$$\sqrt{N} = \frac{r_1 + r_2}{2} + \frac{r_1 - r_2}{2} \cos 2\theta + x \sin 2\theta$$

Graphical method attornath)

Quee 1

A Gest March's Charle method:
A body 18 subjected to dinect

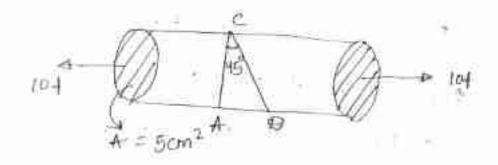
Stress in one dinection:-



step-1 Construct Combinate system and moramou stress is taken along re-axis and shear stress taken iny-axis.

Problem-1

A Cost irran block of 5cm² is
Subjected to a pull of 10 t in one
olineation. Final out the nesultant
stress a plane which is inclined
out an angle of 45° with the



Set ep-1



Force acting on the Cost inten block

= Force = 10t = 0t

Aneo = 5

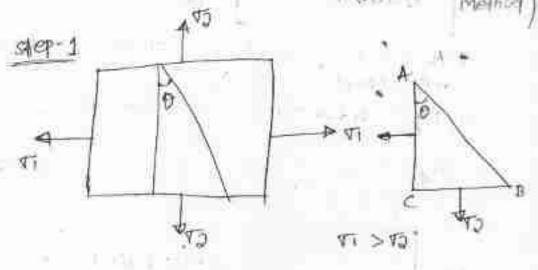
Step-2

Enc. Will gr. Stockers, Atmosphered Links

Telephone to the second of the

Sheart Stress AB = $1 cm = 14 lom^2$ OB = 1.5 cm $(TR) = 1.5 + lcm^2$ $(TR) OA = 1 cm = 1 + lom^2$

Millian perpendicular, shress-



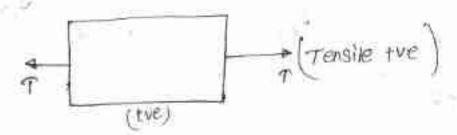
SHEP-2

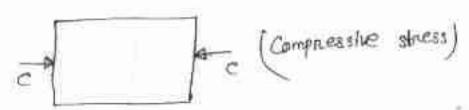
Graphical method to determine the Complex stress in an Inclined plane

Norumal Stress
Pangential Stress
Rescutant stress

- + It is a geometrical method to determinate the complex stress...
- > By offement's we have to

Sign convertion for murch's circlemethod





Tangential on shear striess:

Segn convention for months and method)

+ve -(clack wise)

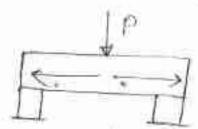
-ve - (Anticlack wise)

> A body is subjected to two musting Penpendicular stress :-1 17 ninde The tensile stress at a point across two mutually perpendicular planes are 120m thod (Tensile) & GON Im 2 (Tensile) Determine the tangential and nesultant striess on a plane at 30° the axix of the minor Stress A Ty . 60 w/mm2 0=300 Фу =60 N /mm2 16m = 10 N / mm 2 3 60 N /mm2 Let F2 = 120 m/mm2 120 m=1 20N /m m2 IC.m = 10 A / mm 2 Circle 00

Bendings of beams

Beam :-

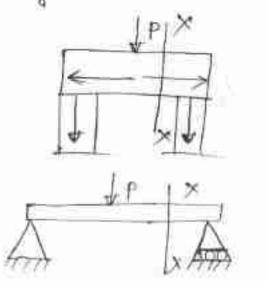
Beams are structural members which are used to triansfer lateral leads / vertical load.

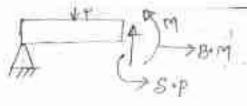


- > suppose consider a beam countying a point local at its Centre.
- > The ventical lead is transfered to the horizontal bearn and finally) transfer to the Colesmin.
- > By the application of this load.

 The B-M and s-F is developed in the beam.
- > If we can cut a section and draw the free body diagram as shown in the fig.

110.94 3





teral

A shear force and bending moment will develop due to this shear force. shear stress will develop.

$$\gamma = \frac{FQ}{Tb}$$

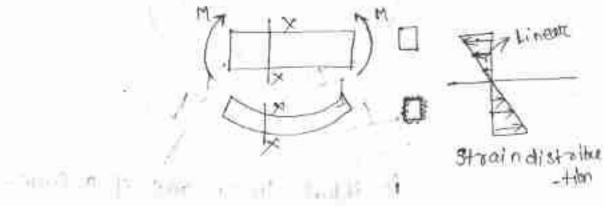
will be devloped. Due to bending STRESS

Gendling Streets '-

The resistance offered by the Internal stresses to bending de benoting stress. is called

for the theory of simple banding

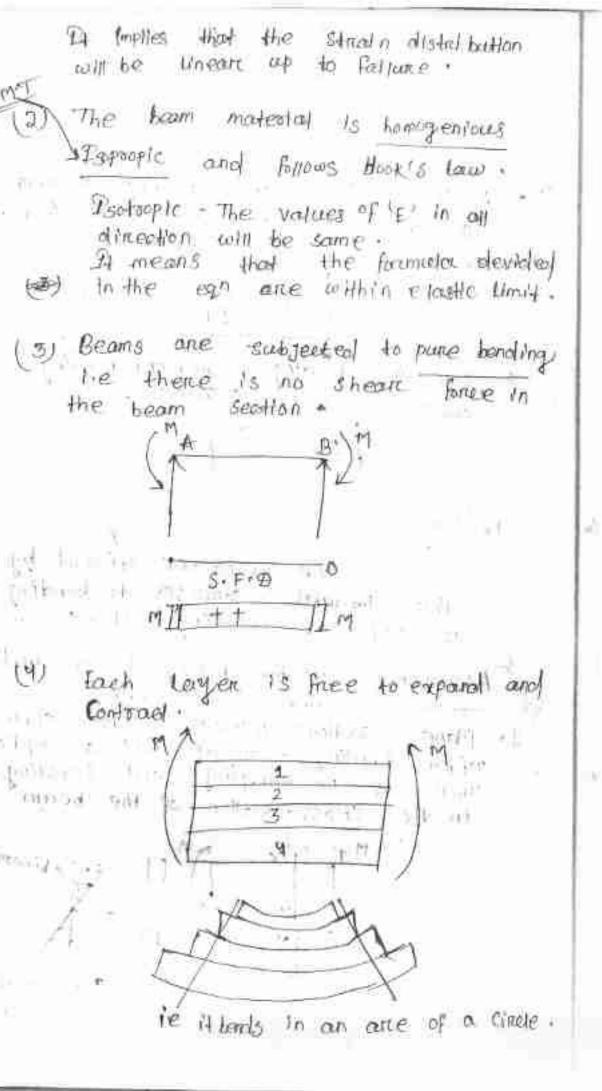
sections memorins plan often bending - As pen this assumption, there is no warping and twisting in the cross-section of the beam

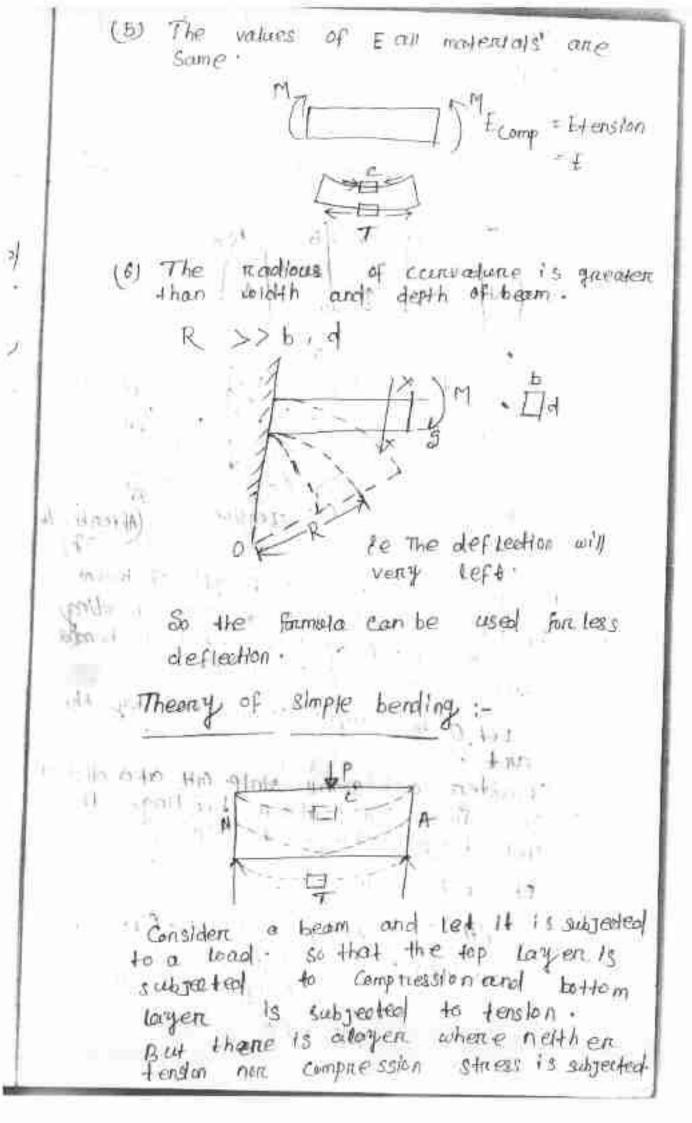


-+10n

en

Đ,





M = TE - E | M: moment of resister.

I M: Moment of resister.

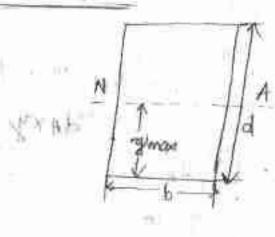
I Moment of resister.

section modulus (Z) :-

It is the route of moment of inestication to moun distance of enthere fibre from

Section, modulus for different sections

O Rectangular



$$Z = \frac{1}{12}$$

$$Z = \frac{bd^3}{12}$$

$$Z = \frac{bd^3}{12} = \frac{ad}{6}$$

$$Z = \frac{bd^3}{12} = \frac{bd^2}{6}$$

$$X = \frac{T}{T}$$

$$N = \frac{T}{T} = \frac{T}{64} 94$$

$$3 = \frac{T}{2}$$

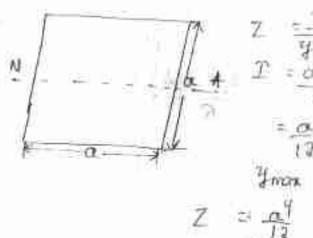
$$3 = \frac{T}{2}$$

$$q_{ij}$$

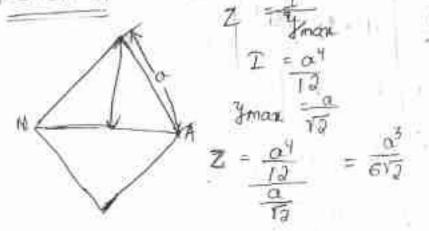
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* Squire

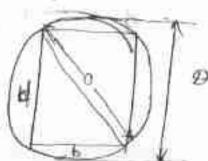


* Diamord



The strongest section in benching.

Ans The strength section
will be $Z = bd^2$ from a cometrical flag by $0 = \sqrt{b^2 + d^2}$



$$\frac{dz}{db} = 0$$

$$\frac{d}{db} \left(\frac{bd^2 \cdot b^3}{6} \right)$$

$$\frac{d}{db} \left(\frac{dd^2 \cdot b^3}{6} \right)$$

$$\frac{d}{db} \left(\frac{dd^2 \cdot b^3}{6} \right)$$

$$\frac{d}{db} \left(\frac{dd^2 \cdot b$$

is simply supported over a spain of your met what uniformity distributed board per mit the beam can conty if the bending stress is not exceed to tanimm ? Take I = 8×106 mmy.

Step-1

500 N

N

L=4nt d= Dom·m.

Step-2

Moment of the beam (d) = 360 m·m.

Spain of the beam (1) = 4m = 400 m.

benoting stress (Tb) = 120 m/mm²

Step=3 $M = \frac{1}{2}$ $M = \frac{1}{2}$

y = DI stance of extreme fibre from N.4 $y = \frac{B}{2} = \frac{300}{300} = 150 \text{ m/m} \cdot \text{m} \cdot$ Let us be the weight on the simply supported beam.

we know that M = VBZ

\$ 2000,000 We = 120×53,334.33

N = 3200 .0

\$\frac{\text{Q3}}{\text{fort a given stress compane the moment of resistance of a beam of a square section when placed.

(x) with it's allogonal sides horizontal.

(b) with it's allogonal horizontal.

PIZ

$$M_1: M_0 = M_1 = \frac{T_1 Z_1}{M_0} \cdot \frac{Z_1}{Z_2}$$

Z, = Seotion modulus of section-I

In = moment of intertacop =

(yman), -> distance of entreme fibre from

$$T_1 = \frac{bat^3}{12}$$
 . $b=a$, $d=a$

$$= \frac{\alpha \times \alpha^3}{12} = \frac{\alpha^4}{12}$$

$$(\sqrt[3]{man})_1 = \frac{a}{2}$$
 $Z_1 = \frac{1}{2}$
 $= \frac{a^4}{12} = \frac{a^3}{6}$
 $= \frac{a^3}{6}$

af

e.

P

ngo

i of

$$\frac{12\sqrt{3}}{12\sqrt{3}} = \frac{\alpha \sqrt{3}}{12}$$

$$\frac{2}{\sqrt{3}} = \frac{\alpha \sqrt{3}}{\sqrt{3}} \times \sqrt{3}$$

$$\frac{2}{\sqrt{3}} = \frac{\alpha \sqrt{3}}{\sqrt{3}} \times \sqrt{3}$$

$$\frac{2}{\sqrt{3}} = \frac{\alpha \sqrt{3}}{\sqrt{3}} \times \sqrt{3}$$

$$\frac{2}{\sqrt{3}} \times \sqrt$$

over the same span and have the same frequency Strength and Compare the weight of these two beams if one of them is solid and other is hollow circular with internal diameter is half of the external diameter.

symmetrical columns with eccentric leading atom enearls :-Zlel p considers a column ABCO subjected to an excen -tale locally about one ands file doctout y-y ends) as shown in the Elevation plan Let p = wood certing on the column - eccontricity of the load b = width of the section : Thickness of the Coleann Area of the section A bd MOI of the seption about 7 4 ans. $I_{XX} = \frac{bd^3}{10}$ $I_{YY} = \frac{bd^3}{10}$ seation moderal $Z = \frac{T}{\sqrt{2}} = \frac{db^3}{\sqrt{2}} = \frac{db^3}{\sqrt{2}} \times \frac{2}{b}$: 1 ab2 Dineral strass on the column due to 6001 40 = f = f

3 +

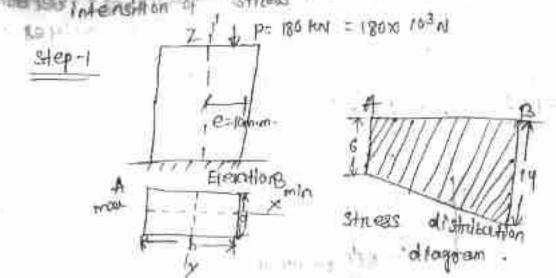
3

Bending stress of any point of the column section at a distance by from y-y and .

$$\sqrt{b} = \frac{M}{Z} = \frac{Pe}{db^2} = \frac{cPe}{db^2}$$

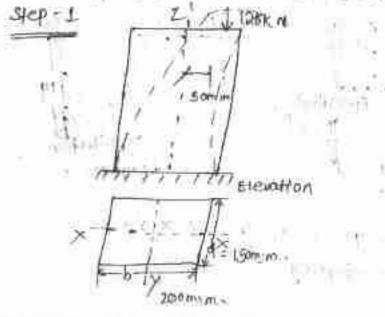
$$= \frac{cPe}{bd \cdot b} = \frac{cPe}{Ab}$$

13 A meeting want street is 15 mm and 180 km 120 mm thick it connies a bowl of 180 km of 10 mm. Ina pane of on the section and min's indistribution of intensition of stress in the Bection.



Width (b) = 150 min. depth (d) = 120 min. Area of the seet on (A) = bx of = 150x120 - 18000 mm2 Tran = 1 (1+ 60) = 180 × 103 (1+ 6×10) = 14 N Jmm2 = 14mpa Trin = f (1 - 60) $= \frac{180 \times 10^{3}}{18000} \left(1 - \frac{6 \times 10}{150} \right) = 6 \, \text{mpa} \, .$ 5 jan zezt

A rectangled continuous comme which one is an thick is continuous a vehicle to the thickness solvent of 150 mm. bending the thickness solvent one the manet and minim entensities of stress in the section.

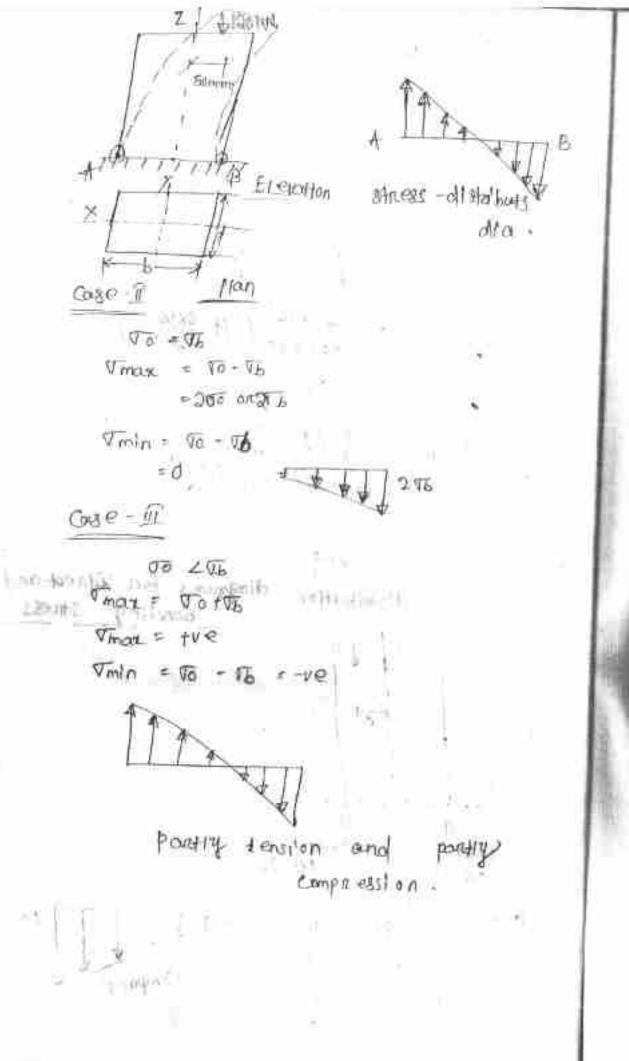


SHOP I Anea of the section - bxd. - 200× 150 -30000 mm2 Maximum Strass = Te (Tb = P + M = P (1+ fe) = 120 × 103 (/+ 6x50) = 16 mpa . . . Trin = + (1 60) 3000 (1- 200) = - 2 mp er Seation distribution diagrams for Direct and bonding smess T min Tmax = TOITE = 10-1h 60 -7b V man Track = (tve)

Tmin = (-ve)

Grypneston

777



Itmy of eccentainity of circular section

(Ixx = Ixx)

ason el

Let us consider a charatan section of diameter 801 x We know that the section modulus.

 $Z = \frac{D_{xy}}{y}$

... 7 · 2 Dxx · II 94

 $Z = \frac{T \times x}{Y} = \frac{T}{64} \times 24 = \frac{T}{33} 23$

Area of cincular seeton

A = \$ 294

For no tension condition :-

e≤ 翡9³

Tal Dax M

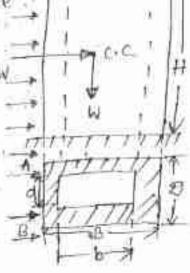
£3

CHIMNEY

Wind PRESENT C (PW)

stress due to wind pressure .

Olineet stress due to self wt = (Ta) = p p -> compressive Locas . due to self-wh.

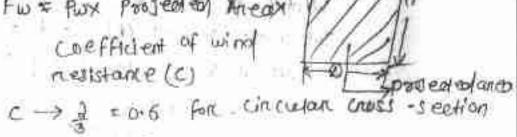


P = WAL] KN where we -> weight density of chimnery material (Kn/m2)

> Croossectional Anea of chimney H = L -> Length of the chimney rd = = wath = wh

Wind force -

FW = PWX Project to Aneax 1 coefficient of wind neststance (c)



c = 1 por fx+ sunface. FW = CX PWX projected anea = 1 × fox (DXH) = fwx DxH kn.

OF. 더

Bend moment @ base
$$M = \left(F_{\omega} \times \frac{\pi}{2}\right) \text{ k.n.m.}$$

$$T_{b} = \frac{M}{2} \text{ y.s.}$$
Section mediculus @ y.s. and s.
$$Z_{yy} = \frac{T_{yy}}{y} \left[y = \frac{B}{3}\right]$$

$$T_{b} = \frac{M}{2} \text{ k.n. } \text{ lm}^{2}$$

$$T_{min} = T_{d} - T_{b}$$

and 1.5 m thick is subjected towind pressure 1200 N/m² find the manum and minm intensities of stress at base if the curit wo of the masonary is as kn 1mb

step-1

Height of the wall (h) = 10 m.

Which ess of wall (b) = 3m.

Thickness of wall (t) = d = 1.5 m.

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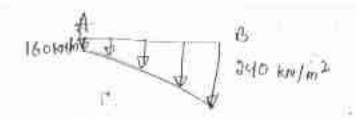
Thickness of wall (t) = 3m.

Thickness of wall (t) = 1.5 m.

Thickness of wa

```
- 20 ×103×10
     ~ 200×103 N /m2
    54 ep<u>-111</u>
             bending stress V6 = 1
        - wind force (FW) :-
       FW = Cx pwx projected Acea
            = 1 × 1200× 9× H
            = 1 × 1200× 1.5×10 .
   Moment @ 6438 M= Fwx H/2
- 90×103 n/m
 section modulus zyy = I yy = db3
 =\frac{6}{1.5\times3^2}=2.25m^3
      TE = 90×103 = 40×163 N/m2
    Trank = Vd + VB
        = 240× 103 + 40×103
          = 240 KN /m2
     Tmin = Td - Tb
```

Tmin = Td - Tb = 200× 103 - 40× 103 = 160 × 103 N /m² = 160 KN /m²



\$ Janes 2021

DAMO

I dom is constructed to stone large quantity of water which is used for purposes of innigation and power generation.

> A dam mary be any crosssection. The following types dams are used in now a days.

(1) Redangular Dam

100

PITrarizoldal damshaving water

Water

(3) Troopizoidal dams howing water face inclined

terren h

(4) Rectangulare Gams: .-

Consider o unit tength of a rectangular dom to metaining, water to vertical side on show in fig.

In fig. A = 70eLet $b \rightarrow w$ width of the clam B = he e e e B = he e e

S -> specific up of the clam masonary h -> Height of water negatived by clam.

weight of the damper unit Length

w = 36h

The weight wi will act through centre of gravity of clam section. The intensity of water pressure will be zero on the water surface and will increase by a smalght whe Low to what af the bottom.

Thus and intensity of pressure on the fall of the dam

Pang = $\frac{6 t \, \text{wh}}{2}$ = $\frac{10 h}{2}$ Total pressure per unit length of the dam = $\frac{1}{2} \times \text{wh} \times h$ = $\frac{\text{wb}^2}{2}$

This water pressure acts of a height of his from The bottom of the

H.

Now The negutiant of water pressure and weight of the obm will be given by $-R = \sqrt{t^2 + W^2}$

the contre of gravity of the dam and the point through which the scentillant R cate the base

From similar trilongles.

of dam's where the nesultant cut the base

eccontrol city of resultant. e = d - b/b

- Mangitude of moment

$$T = \frac{1 \times b^3}{12} = \frac{b^3}{12}$$

r blad was a district on out

$$Z = \frac{1}{7} = \frac{b^{3}}{\frac{12}{b}} = \frac{b^{3}}{12} \times \frac{2}{b} = \frac{b^{2}}{C}$$

$$Th = \frac{11}{7} = \frac{W}{b^{2}} = \frac{6We}{b^{2}}$$

$$Direct stress = Weight of dom$$

$$= \frac{W}{b}$$

$$Timer = \frac{W}{b} \left(1 + \frac{6e}{b^{2}}\right)$$

$$= \frac{W}{b} \left(1 + \frac{6e}{b}\right)$$

$$Timer = \frac{W}{b} \left(1 + \frac{6e}{b}\right)$$

$$= \frac{W}{b} \left(1 + \frac{6e}{b}\right)$$

9 Janua 2021

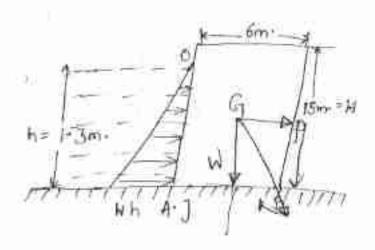
10

A concrete dam of neelangulan Section 19 m. high and sm. wide Contains water upto height of 13m. find

- o total pressure perent (Length of the dam
- point where the resultant Cut 1 The the base
 - @ Max" and min" intensities of stresses at the base

Assume with what waters and concrete as 10 and 25 KN/m3

KI 1 (1 36)



3+ep-11

Width of the dam(b) = 6m.

Height the dam(H) = 15m.

cunit wt. of woder (Lu) = 10 km /m³

cunit wt. of concrete & = 25 km /m³

- (1) Total pressure per mt Length of dam s $P = \frac{1}{2} \times \omega h \times h$ $= \frac{1}{2} \omega h^{2} \ln h$ $= \frac{1}{2} \times 10 \times 13^{2} = 845 \text{KN}$
- (11) point where the Resultant Cuss the base:Weight of the dam per mt length
 W = Jxbx+1 = 25x6x15 = 2256 kN

$$nx = \frac{P}{N} \times \frac{h}{3}$$

$$= \frac{845}{2250} \times \frac{13}{3} = 1.627 \, \text{m}.$$

17253

(11) Max'm and min'm intensities of atmess

eccentricity of the resultant
$$e = x = 1.627m$$
.

$$\nabla m_{art} = \frac{10}{b} \left(14 - \frac{6e}{b} \right)$$

$$= 2250 \left[14 - \frac{6\times 1.633}{6} \right]$$

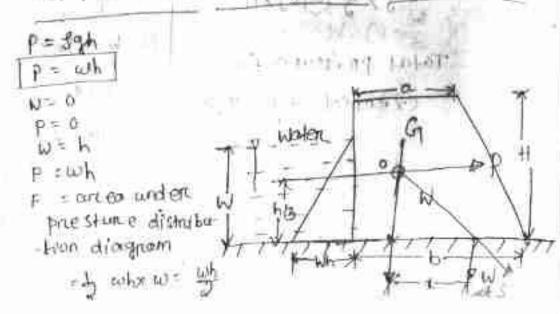
$$Tmln = \frac{W}{b} \cdot \left(1 - \frac{Gv}{4}\right)$$

$$= \frac{3256}{6} \left[1 - \frac{6 \times 1.623}{6}\right]$$

953-625 MA 983-625 KN/m²

1 graph e-rit et e _ g G .

Trapezoidal dams with water face ventical :-



Consider a unit length of trapezoidal dam having HS water face ventical as sharing in Ag .

Let a - Top width of the dam b = bettom width of the dam H = Height of the dam f = conit of of down masonary

The weight of the dam per unit Length = 3 × (atb) × H

pressure on a cont length of dom P = ± x whxh

= whz

11 January 2021

West of the dam per unit length

= 1 x + (a+b) x H

Sm = 121

Total pressure force exented by worten ジ W=JmV = Smx4x = gmxA =JM×J (odb)xH Kin In

The horizontal distance bean cog of the dan and the point at which the resultan--t cuts the base (nc) 2MJ =0 Px h/3 - Wxx = 0 > px = = Wa > 1 = f ×h15 The distance bet a and the nescultant cut the base d' d = AK +KJ = AK 代表 *专) At the $\bar{a} = a^2 + ab + b^2$

3 (atb)

Eccentricity (e) = d - = - Man 3tress at B \sqrt{max} at $13 = \frac{W}{b} \left(11 \frac{6e}{b}\right)$ Timin at A = (1-68) PER TIME

12 A Concrete dam of trapezdidas seether having water on ventice force is 1cm. high . The base of the dam is sm. wide and top am wide Find the (a) resulting force trust on the base permt Longth of dan the point where the negultary through custs

Take unit where concrete of as kn made and the water level coinciding with the top of the claim.

<u>So∩</u> step-1

Step-11 The top width of the dam (a) = 3m.

Bottom width of the 11 (b) = 8m.

Height of the dam (H) = 16m.

Height of the water metained by

the dam (H) = 18m.

conit cut of concrete if, =25km/m3

conit cut of coortex cul =9.81km/m3

Step-III The rescultant from on the base per my Length:—

weight of 1 the dam per unit length $W = 5 \times \left(\frac{3+8}{2}\right) \times 16 = 2200 \text{ km}$ water force par mt length of dam $= \frac{1}{2} \text{ wh}^2 = \frac{1}{2} \times 9.81 \times 16^2$ = 125.06.68 km

 $R = \sqrt{p^2 + \omega^2}$ $= \sqrt{(255 \cdot 68)^2 + (2200)^2}$ $= 256 \ 2533 \cdot 12 \ \text{KN} \ .$

mis 41

16

step- iv The point where the resultant Cuts the base.

Taking moment area (*Im-

about 1 (16×3)+ (=×5×16) ×A]

= (3×16×3)++ ×5×16× AF 4] (31 mm)

=> 88 AJ : 258 17

AJ = 258.7 = 2,94m.

 $AJ = \frac{a^2 + ab + b^2}{3(a+b)} = \frac{3^2 + 3 \times 5 + 5^2}{3(3+5)}$

= 2.04

The horizontal distance bet the confine of growity of the dam section and the poin where the resultant cut the base . 1255.68 x 16

7 = 3.04m.

d = AJ + x = 2.94 + 3.04 = 5.98

Intensities of maxim and minim stress at eccentricity (e) = d- =

= 5.98 - 3 = 1.98

3

80

$$\frac{1}{8} \left(1 + \frac{6e}{6}\right)$$

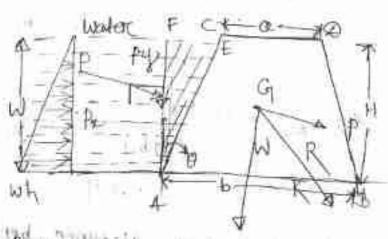
$$= \frac{3200}{8} \left(1 + \frac{6\times 199}{8}\right) = 6008$$

$$\sqrt{\frac{8}{8}} \left(1 - \frac{6e}{6}\right)$$

$$= \frac{100}{8} \left(1 - \frac{6e}{6}\right)$$

$$= \frac{100}{8} \left(1 - \frac{6e}{6}\right)$$

Trapezoidal dams with Water fall inclined



Pu = Paing - P

Ty = paine

Consider a unit length of claim trapezoiday in section as shown in the Aguire having water face incland.

tel a -> Top width of the dam. b > bottom width of the dam # -> Height of the dam 5 -> unit wt of dam masonary h -> Height of water netain and

tue -> Unit width of water. 0 -> Inclination of water face with v erth (ce) 3. So length of sloping side LE which is subjected to under pressuring mz (AE = B) Coso - AF 4 $\Rightarrow \cos \varphi = \frac{\omega}{L}$ MIM $\Rightarrow a = \frac{b}{a}$ 712/ weight of the dam periunit length W - J x (45) XH so the intensity of water pressure will be zero of the water sunface and will increase at the bottom wh - Total pressure force on a unit length of dam p = + whx ! = + whi The pressure force and a height of his from the bottom of thedam. Horizontal component of this wastern pressure PH = P cosp = whe x + = whi 301vertical component of this water pressure 0 PV = Psino = whe x EF = y x Ef x h = weight of the wedge AFE The distance best centre of grantity of dam section and the point, The the attent and the base . 311

DA

Tatal stress of the base of B

Total stress the base of A

Total stress the base of A

$$=\frac{W}{B}\left(1-\frac{6e}{B}\right)$$
A water fank contains 1.3 m

sol 4 water fank contains 1.3 m deep water find the pressure excepted by the water per mt bength of clam.

Sol - Height of the water (h) = 1.3 N

priessure (P) = #

p= 39h = wh wh w -9.81 KN/m3=9816461

 $\frac{1}{2} \times b \cos x \text{ height}$ $= \frac{1}{2} \times b \cos x \text{ height}$

total pressure exerted by the waters $P = \frac{wh^2}{2} = \frac{9.81 \times 1.3^2}{2} = 8.28 \text{ kN}$

Find the mangitude and line of about on of the priessure exercted on the side of a tank which is in square and limb deep the tank is filled half full with a

is the the reminder is filled with a required having spignofigi Toke specific with of water localims 5011 F Elevation whiz Date given :side of the squire tank (a) = 1.5m. Depth of the tank (W) = 1ml Depth of Spgn of the = 0.5m. Depth of sop gar 1' 12 queld (hi) = 0.5 m. Unit we of worter (wa) = 10 km/m3 Manglitude of pressure: Intensity of pressure of 10) = (SE) = Wih , = (lox1)x05 = 5kN Sp gravity 1 = unit int of regulal 1 unit wt of water otype = 1 = unit of reguld g 10 Km / m3

WHI

> Unit wit of liquid . 1 = (1 × 10) KN/m3

+ stal pressure force of liquid (spgral)

(A) = Area of pressure diagram x length

of the tank

= = = > xw1h1 × h1 × 1.5 = = = ca1h12 × 1.5 = = = w1h12 × 1.5 = = = ×6×1.5×0.5 = 1.875 kN.

Priessure force at c' alue to spign 1 =

Anea of nectangle DEFC × Length of

tank

= wihi x hz x05

, = 5.0 ×0.5×1.5 = 3.75 KN

Intensity of pressure of 181 due to sp. gr. 10° = with 2 = 20 x05 = 10 kN/m² with 2 = 30 pr. x unit with water

= 2×10=20 Kn1/m3

pressure force due to liquid of sp.

gra 2' p3 = Area of trulangle EFBX

Length of tank

= = = x w2 h2 × h2 × 1.5

= = x 10×0.5× 1.5

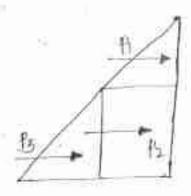
= 3.75 KN.

" Mangetude of total force

P = Pi+P2 + P3

= 1.875+3.75 +3.75 = 9.375 kN

Whe of action of negutiant force:-



15 Janu 2021

Stubility of dam 1-

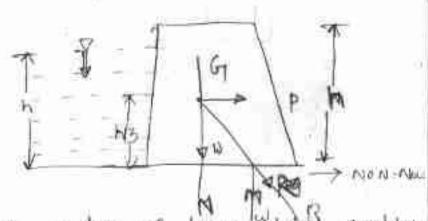
A dam should be stable many four tonditions But the dam By studying on the soil on which

@ By over turning

3 Que to tensile striess developed.

1 Que to pacessive compressive stress .

Condition to prevent the stiding of thedonis



Consider a dam of thospe zoldas section Height H and having water up to a depth of hi The force acting on the dam one

@ Force due to water pressure p acting horizontally at a height of & above the base.

of the dam 'we' acting werth can you acting werth can y down, word through the CG of dam.

So the trescutant force of and we point my the point on the point of the dam will be in equalibration of the point of in the opposite direction of the point of in the opposite direction of the point of the reaction of the dam the reaction of can be resolved in to two components the ventical component of the horizontal component will be equal to furctional force at the bouse of the dam

P = Francis = New

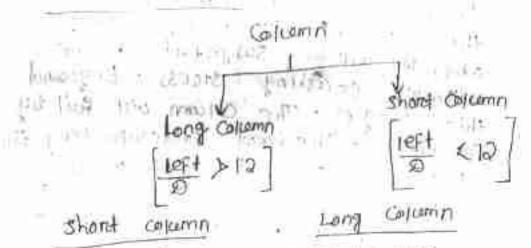
Fmax > NN

Struct 1- A Structural member subject of to an arial compressive force is called as stud.

> A strice many be vertical horizontal or inclined .

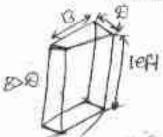
A vertical struct is called as column which is used in building forcomes.

Tapes of column



Deffective length LID effective length >10

Least lateral length Library | Teast Lateral chimension



2 will be taken

caushing . - K45

1eft < 45 1eft >45 remin . THE PROPERTY OF THE

* shoret concern fails by truckling

5.941

10%....

*semleraness reation * senderaness runtion >45

when a ceremn is subjected to samp compressive force. The compressive stress induced

72 = A

P7 Compressiv Force

A + Chass-seational Area of allumin.

A Lettle Consideration will show that if the Load is gradually increased the Collemn will reach a stage when it will be subjected to the withmate crushing stress. Beyound this stage The column will fail by Crushing. The Load corresponding the crushing stress is collect crushing the crushing stress is collect crushing.

does not feel by crushing.
but also by bending i.e buckling.
The load of which the column just to
buckle is couled buckling local on

Assumptions of Evelour's column theory:

1) Initially the column is perfectly attack and the lossel applied is

(3) The dross-section of the Glumn is centiform throughout 4s length.

(3) The Column material is perfectly come, homogenious and Isotropic , obeys bookes Law. ys The length of column is very large as componed to its cross-section. (3). The shadening of columns due to olinect compression is neguerated. (6) THE failure of collemn occurres due to builting only. Types of and conditions of concerns. @ Botherds himged . Both ends fixed @ one end is faced and other end is hinged . (9) one end is fixed and other field. Columns with both ends hinged s-Consider a Colcenn AB of eength & hinged at both of 1416 ends A' and B' catalying o outlied lood by deficials into a concred from AXB Now concident amysection (x) at a distance From 41 let p -> critical Load on column of of deflection in the column at (1) Moment clue enultical local p

280

à

20

Column 1- It is a structural member which is subjected to ordal Compressive load.

Street :- It is a streetestal member - cuhich i's subjected to actal Compae ssive load - H many be hontzonfail on Indined on vertical.

> The vertical struct is colcenn

Stendenness nation (s)

It is the route bett effective length of column and minim madious of gynation.

· Lefa [Cmin

A remin = I Tremin = = = =

Column

Shoret colcumn

5 <30

> falls by caceshi'ng

nut les V Mollan @ EMM

30< 5 ×120

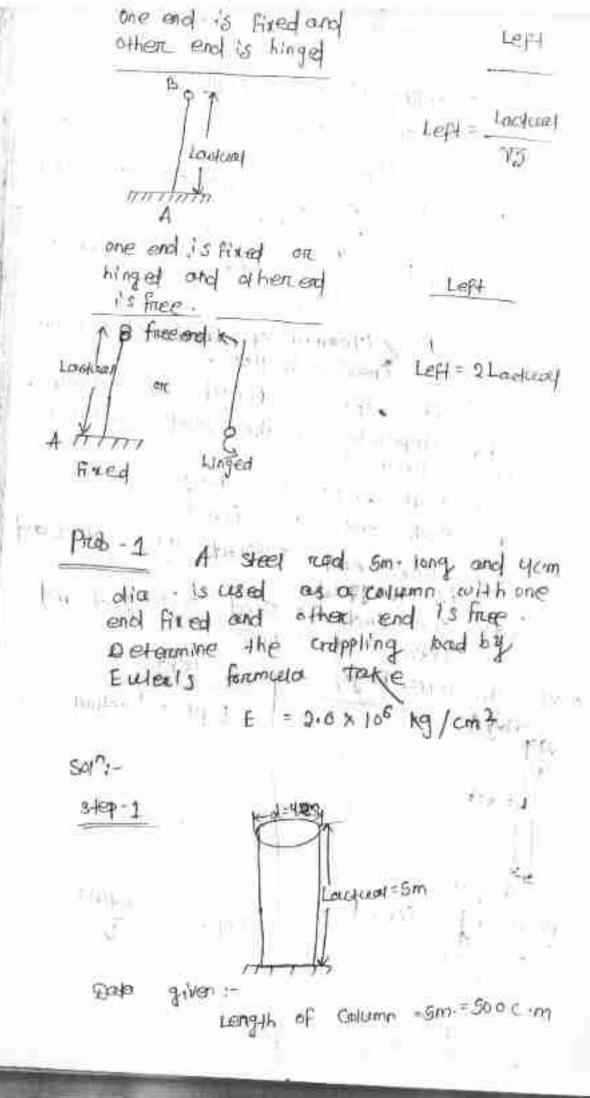
> falls by enushing on buekling

Trots

Long column 5 >120

Long column falls buschling,

```
Euler's forumula for long, column:-
            (P) contippling I buckling I conticol
              . = TTO E I min
                      LZPH
              Where E > youngs modules of akomn
                         maderial.
                    I - (I xx, Iyy) min of In and
                         Ty4
                  I -> Moment of Institutof, column
                     cross - section .
h
               Left - effective Length of column.
            Left depends on the end condition
            of column :-
            (a) Both ends are hinged
           (b) Both ends one fixed
            co one end is fixed and other and
                is kingged.
                one end is freed on hinged and
               other end is free. Left
       Both ends are hinged
                         Left = Ladual
          > himed
                                        1760
          Laokes
415
         Shinged
       1301 h ends fixed
             Locket .
```



Dia of column = 100 ycm. Imin = mill of Ixx and Igg Ixx = T x44 = 47 cmy Tyy = T xy" = 49 cm4 So Both the values one same, We can take any one of them. Ixx = 4TT cmy E = 2.6 × 10 Kg lam2 Perippling Tep So we know that when one end is fixed and other send is free. Left = 2 todual . = 2× 5000 m = 1000 Cm Percippling - (1000)2 = TP × 2.0 × 10 × 411 (1000)2 = 248 . 05 kg Ans Rankine's Francela for medium Glumn and short coleum!-Rankine's formula is given by pr = pc+pE

Pre > Crushing load = TCA

Pre > TI 2 EJ Cripping load by eluen's

Pre > Tieff Cripping load by eluen's

$$\frac{1}{PR} = \frac{1}{Pc} + \frac{1}{Pc}$$

$$\Rightarrow \frac{1}{Pn} = \frac{Pc PE}{Pc}$$

$$\Rightarrow Pn = \frac{Pc PE}{PE + Pc}$$

$$= \frac{Pc}{1 + Pc}$$

$$= \frac{Pc}{1 + \sqrt{c} A} \times \frac{1}{1 + \sqrt{c} A}$$

$$= \frac{\sqrt{c} A}{1 + \sqrt{c} A} + \frac{1}{\sqrt{c} A}$$

The real Printings of

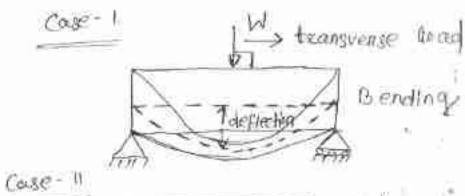
IRMANIA A PROPERTY.

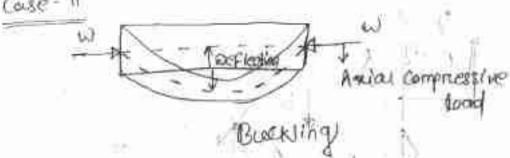
not by the son

OTT OT ---Walt spech

a fight and of second services to

slope and deflection of elastic beam



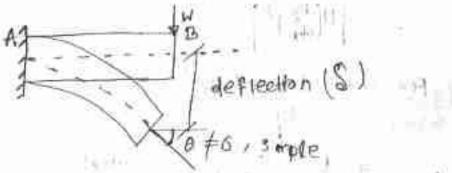


Bending - The deviation of axis due to transvense Local is called bending.

Buckling. The deviation of axis due to

Axial compressive and is called

as buckling.



Deflection: - It is the Linear deviation of axis under bending is called as

It is denoted as S. it units is mm

Stope 1- It to the angular downton of action under benefing is control of 7645 > It is denoted by (a) > It's unit is modian degree. Frame of reference:y = deflection of from elementary controlly $\frac{1}{R} = \frac{d^2y}{dx^2}$ $\frac{1}{[1+(\frac{dy}{dx})^2]}$ $\frac{1}{[\frac{dy}{dx}]^2}$ For small defrection We know that $\frac{d^2y}{dx^2}$ $\frac{d^2y}{dx^2}$ $\frac{d^2y}{dx^2}$ $\frac{E}{R}$ $\frac{E}{R}$ $\frac{E}{R}$ $\frac{E}{R}$ $\frac{E}{R}$

$$\frac{d^2y}{dx^2} = \frac{m}{ET}$$

$$\Rightarrow m = ET \frac{d^2y}{dx^2}$$

$$\Rightarrow \frac{d}{dx} (m) = E T \frac{d^3 y}{dx^3}$$

$$\Rightarrow F = E T \frac{d^3 y}{dx^3}$$

The stope and deflection of beam may be derived by following method.

1 Docable intigration method

@ Maeselayis meethod.

Queble intigration method:

$$M_x = EI \frac{d^2y}{dx^2}$$

$$\Rightarrow E \hat{I} \frac{d^2 \hat{I}}{dx^2} = -M$$

$$\Rightarrow E \hat{I} \frac{dy}{dx} = \int -M dx$$

$$\Rightarrow E \int \frac{dy}{dx} = -mx + C, \qquad 0$$

$$\Rightarrow E \int y = \int -m \ln x + \int C_1 dx$$

$$= -m \int x dx + C_1 \int dx$$

$$= -m \int \frac{x^2}{2} + C_1 x + C_2$$

$$= -\frac{mx^2}{2} + C_1 x + C_2$$
for Calculating the value of $C_1 \otimes C_3$

$$E \int \frac{dy}{dx} = -mx + C_1$$
when $x = 1$, $\frac{dy}{dx} = 6$

$$\Rightarrow 0 = -mx + C_1$$

$$\Rightarrow C_1 = Mx$$

$$E \int \frac{dy}{dx} = -mx + C_1$$

$$\Rightarrow C_1 = Mx$$

$$= -mx + m_1$$
when $\frac{dy}{dx} = \frac{mx}{2} + \frac{mx}{$

Case-II

$$\frac{d^{2}y}{dx} = 0$$

$$\frac{d^{2}$$

Ž,

When
$$x = 0$$
 and $y = 0$ month C_8

If C_8 and C_8 and C_8

If C_8 and C_8 and C_8 and C_8

If C_8 and C_8 and C_8 and C_8

When C_8 and C

1 156 2001 GSE-11 and deflection of a simply slope beam contrying a point of its Support en centre :-Consider a simply supported beam AB! whose span is land countying a point wood at 1415 centre. Let RA and RB be the repullment 41 8 81 moment at 1.1 Taking EMM = Q T. A.M = T.C.M > R8×x = wx 4/2 · NB=当 70.1 = T. D.L ≥ RA = W-RB = W- J = W > Consider a seation x-x atadistance of from A! mx= RAXI = 当XI = d274 = Max maclious of curvocaume) BD. daz $ET = \frac{o(2y)}{1} = \frac{u_2}{a} \propto$

FI =
$$\frac{dy}{dx} = \int \frac{dy}{dx} + \frac{dx}{dx} = \int \frac{dy}{dx} = \frac{\omega}{2} \int x dx$$

FI = $\frac{dy}{dx} = \frac{\omega}{2} + C_1$

FI = $\frac{dy}{dx} = \frac{\omega}{4} + C_1$

FI = $\frac{dy}{dx} = 0$

FI =

when
$$r=1$$
 $\frac{dy}{d1} = 0 max$

$$\Rightarrow ET 0 max = \frac{\omega k^2}{16} + \frac{\omega k^2}{16}$$

$$\Rightarrow ET 0 max = \frac{3\omega k^2}{16}$$

$$ET y = \frac{\omega k^3}{18} + \frac{1}{16} + \frac{1}{12} + \frac{1}{16} + \frac{1}{12} + \frac{1}{16} + \frac{1}{12} + \frac{1}{16} + \frac{1}{16} + \frac{1}{12} + \frac{1}{16} + \frac{1}$$

Case-D

supported become countying uniformity distributed become over the entire Length of beam 1-

RA LUZ L LO RE - W

Let us consider a simply supported beam

Let it is subjected to a least worth/kun (u.d.1) over the entire length.

Let RA & RB be the neartion at 1 and B'
To find out the neartion RB
Taking moment at 1 i.e EMA = 0

TOTAL OF TOOM

> T.A.M - T.C.M > RBXX = WXXJ >> RB = w1 T.U.L = T. D.L > RA + RB = W6

> Rx = W1 - RB > W1 - W1 = W1 2

Let us consider a Section a-a at a distance a firem A Mx = RAXX - Wix . x Ma = W1 x4 - W1 2 from relation slope deflection radious of curvature relationship Mac = Eloloy > EI d2y - 1 7 - wa2 \Rightarrow EI $\frac{dy}{dx} = \int \left(\frac{uy}{2}x - \frac{ux^2}{3}\right)dx$ = we frate = fx2dq = w1 x2 - wx3 + QG-ET dy = w1x2 - wx3 + 61 -> EIY = [[wx2 - wx3+c,] dx = WI fredr - w fredr + Scidr

10

3'

= wx [= 3] - w] + c, [] + c, = WLA3 - Wx4 +CIX +CD - Odeflection

$$y = 0$$

ET
$$\frac{dy}{dx} = \frac{\omega x^3}{48} - \frac{\omega x^3}{48} = 0$$

ET $\frac{dy}{dx} = \frac{\omega x^3}{48} - \frac{\omega x^3}{6} + C_1$

$$\Rightarrow 0 = \frac{\omega x^3}{18} - \frac{\omega x^3}{48} + C_1$$

$$\Rightarrow C_1 = \frac{\omega x^3}{48} - \frac{\omega x^3}{16} = \frac{\omega x^3}{48}$$

$$\Rightarrow C_1 = \frac{2\omega x^3}{48} - \frac{\omega x^3}{16} = \frac{\omega x^3}{48}$$

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$$\Rightarrow C_1 = \frac{2\omega x^3}{48} - \frac{\omega x^3}{16} = \frac{\omega x^3}{48} = \frac{\omega x^3}{24}$$
ET $\frac{dy}{dx} = \frac{\omega x^3}{48} - \frac{\omega x^3}{24} = \frac{\omega x^3}{24}$

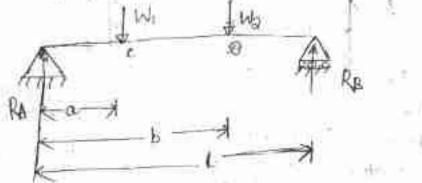
when
$$x=0$$
 $\left(\frac{d^3y}{d^3x}\right)_A = 0$ max at $y=0$ $\frac{d^3y}{d^3y}$

$$\Rightarrow E\Omega \quad 0 \text{ max at } A = -\frac{a_1A^3}{2y}$$

$$\Rightarrow \quad 0 \text{ max at } A = \frac{a_1A^3}{2y}$$

Meachay's method to find out the stope and deflection of beam :-

Ma= Raxa



 $M_{\infty} = Ra \times x - W_1 (x - a) - W_2 (x - b)$ Therem I terem

O If the deflection and slape that it and condition be consider in the momenting.

1st term will be consider in the momenting.

(1) If the slope and deflection bet?

(1) If the slope and deflection bet?

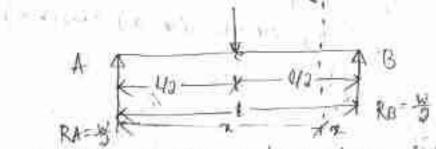
(2) Is to be calculated the show is to be consider.

- (III) of the stope and deflection but n (D) and (B) is to be Colculated Then up to III rol town will be Considered in the moment en
- (m) Intignation constants, should be adoled in the 1st form only.

 Mx = Roxxt C1 W(x-a) W2(x-b)

* Stope and deflection of a simply supported bearn Carrying a point want and its contre .

(Maedicing is method)



Let us Consider a been simply supported beam Countying a point local Wice its centre and the length of the beam AB 1811

Let it is subjected, to a point load

EP
$$\frac{d^2y}{du^2}$$
 = Mx
DET $\frac{d^2y}{du^2}$ = $Raxx_1 - W(x - Ua)$
DET $\frac{d^2y}{du^2}$ = $\int Raxdx_1 - W(x - Ua)$
DET $\frac{d^2y}{du}$ = $\int Raxdx_1 - \int W(x - Ua) du$
DET $\frac{d^2y}{du}$ = $\int Raxdx_1 - \int W(x - Ua) du$
= $Rax\frac{u^2}{u} - W\int (x - \frac{1}{2}) dx$
= $Rax\frac{u^2}{u} + C_1 - W(\frac{u - \frac{1}{2}}{u})^2$
ED $\frac{d^2y}{du}$ = $Rax\frac{u^2}{u} + C_1 - W(\frac{u - \frac{1}{2}}{u})^2$

6 feb 2021

5

(14)

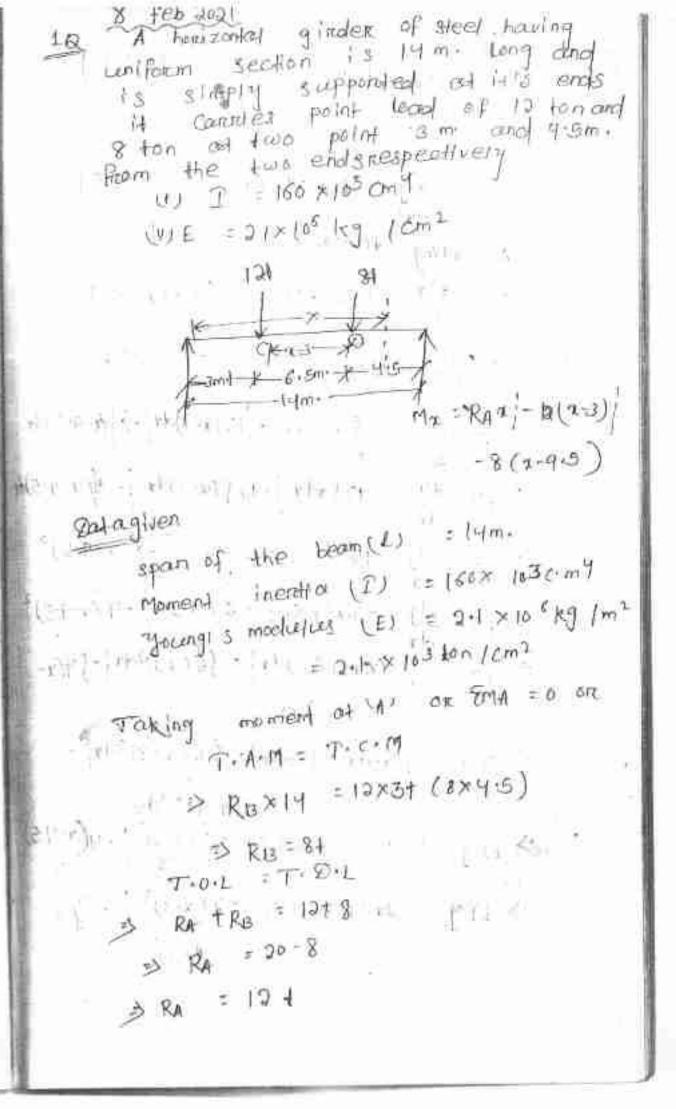
K1 A beam of Length em is simply supported at it's ends and cannies two point Lected's cle KN and yo KN at a distance of and and ant nespecti - very from left support find.

- @ deflection under each Load
- in the point at which man's defication

E = 2×105 11/mm² and 17 = 85×10° YORN -6m - ---

Company of the compan

The state of the state of



As a result of this tonque 71 the shaft end 681 will notate clock wise and every cross section of the shaft.

1 114 2 114

Let R = Rodius of the shaft

L = Length of the shaft

Y = shear stress include of the surface of the shaft.

C = Modalus of regionity of the motorion of = m1909' equal to shear strain of twist

Now distantion the outer surface due to manager To = 99' shear strain of the outer surface

 $= \frac{D \cdot 9'}{C \cdot 9} = \frac{D \cdot D'}{L} = +an \frac{1}{19}$ $\neq + s \text{ very Very Smal})$ $= 30 + an \rho = \rho$ $= 3D' = \rho \text{ equation } \bigcirc$

as = Distination per unit length

shear strain of the outer surface p = 20 1= 100 Ane length = 00 ×0 . CDD" = R x t put the value egn DDI in egn D 0 = RO the moduluse of nightly ci of the material of shaft. c = shear shees produced shear shear produced RO (= XXL) $\frac{1}{R\theta} = \frac{S\theta}{L} = \frac{\chi}{R} = \frac{2}{R}$ $\frac{2}{R} = Constant$ 19913 the sheer stress inducted at a nodious of in from the contre. Y = 9 R CB

ial

aln

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Define poisson's natio

\$1271 is the mate of laterial strain to the theorem Steelin :

> Linear strain is the Painting strain which is tensive in roture then the secondary smain is compressive in nature then the secondary strain is compressive in minute.

As = finemal strain on trian verse strain . I'm Linear or primary strain

01

Bib) what is the point of contrafference of I In a beam the point of where the bending moment changes the sign-

At the paint of control flexure bonding moment 5 ZERLO

> At the point of control Flexure the born flexus is apposite direction

> I) is also otherwise known as point of oflewion .

5) Define Footon of safety

the D is otherwise known as exterly charter. It is defined as the matta of absolute strangth to actual offlied book

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